

# Structure of Ca isotopes between doubly closed shells

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# Collaboration

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*Institut für Kernphysik, Universität zu Köln, Köln, Germany*

G. de France et al.

*GANIL, Caen, France*

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W. Urban et al.

*University of Warsaw, Warsaw, Poland*

D. Bazzacco, D. Mengoni et al.

*Università degli Studi di Padova, Padova Italy*

A. Türler et al.

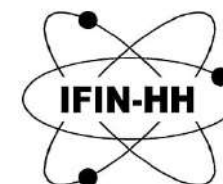
*Univeristät Bern and PSI, Villigen, Switzerland*

Y. Niu

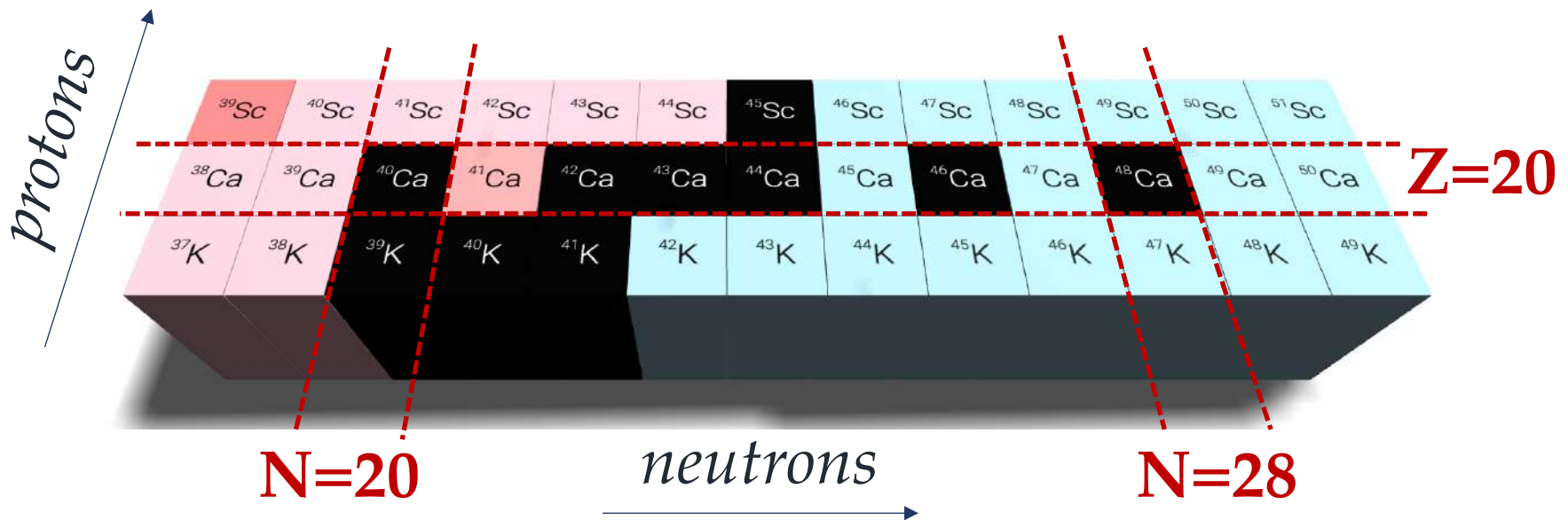
*Lanzhou University, Lanzhou, China*



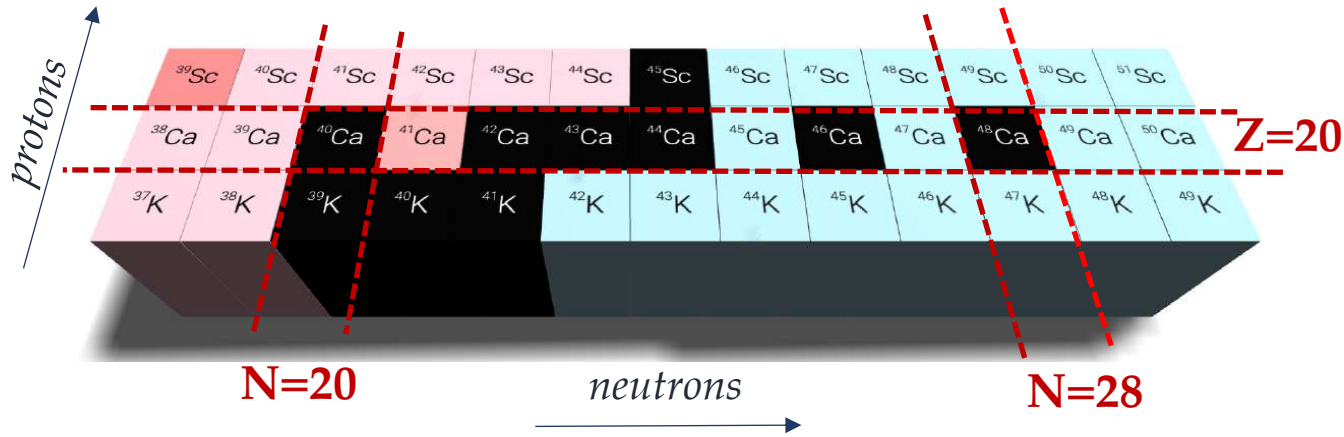
Istituto Nazionale  
di Fisica Nucleare



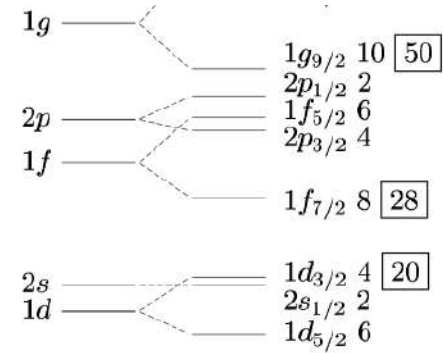
# Introduction



# Ca isotopes: coexistence of complex structures

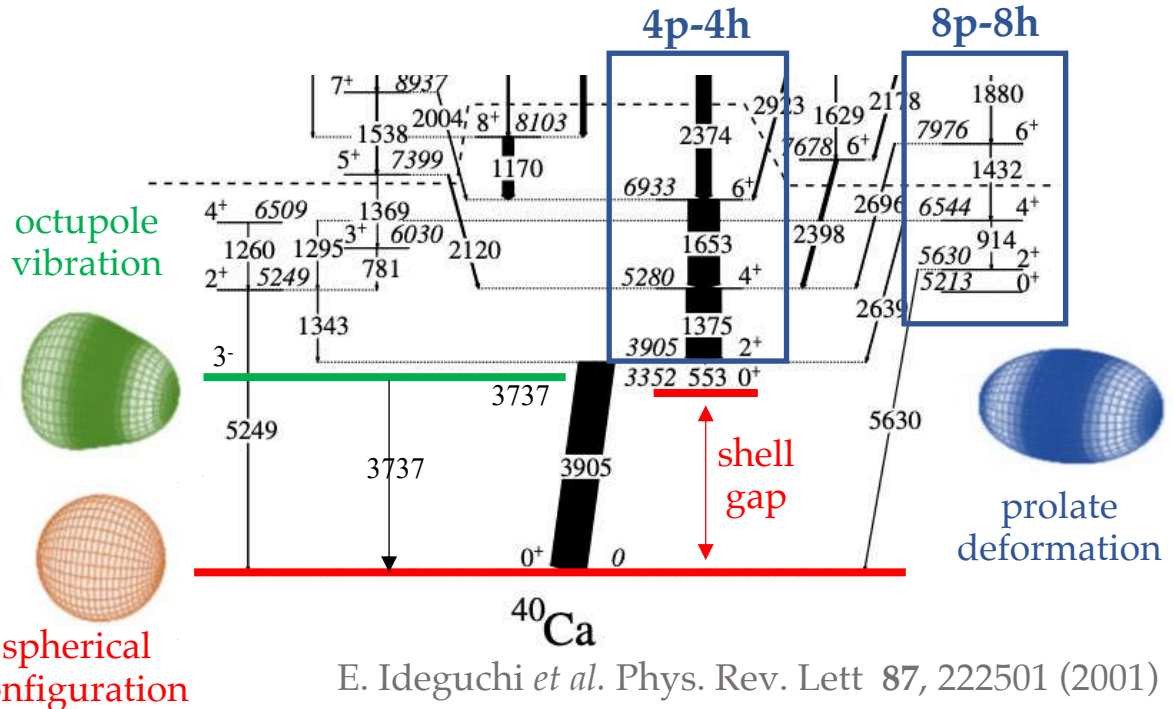
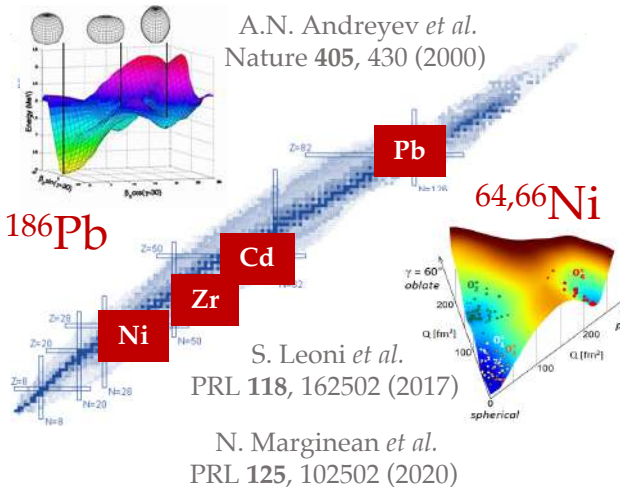


## Active $\pi$ - $\nu$ shells



## Evolution of complex excitations from symmetric to neutron-rich nuclei

### Shape coexistence across the nuclide chart

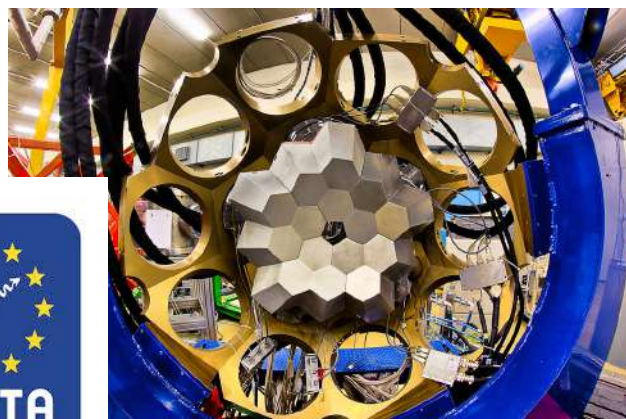


# Ca isotopes: coexistence of complex structures

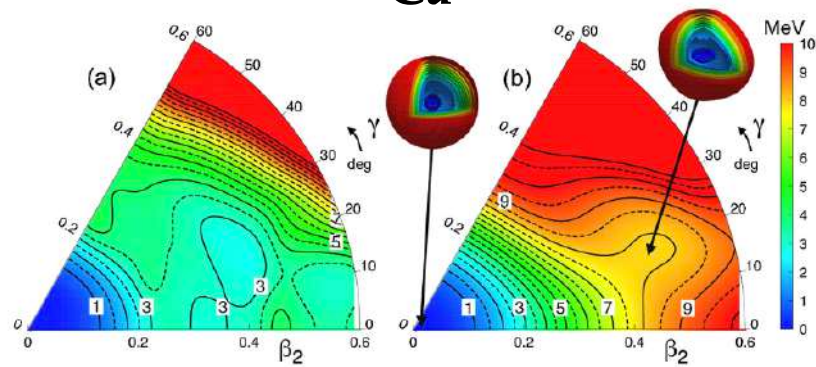
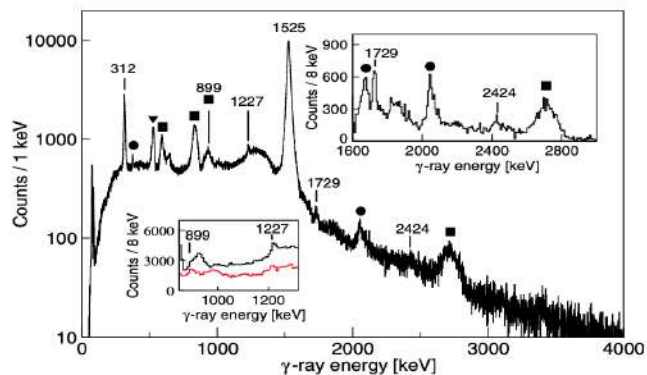
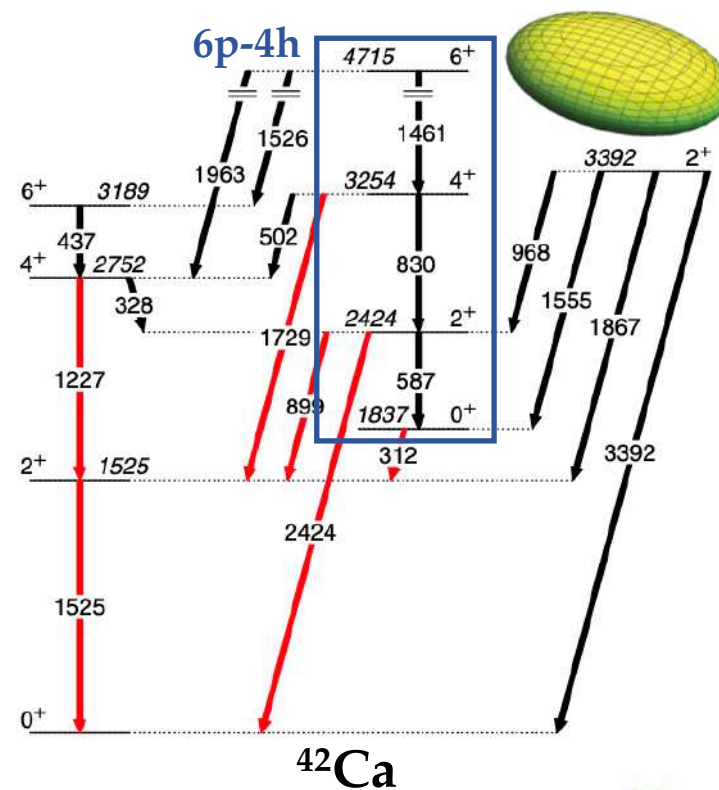
## SUPERDEFORMED AND TRIAXIAL STATES IN $^{42}\text{Ca}$

### COULOMB EXCITATION @ LNL

$^{42}\text{Ca} + ^{208}\text{Pb} / ^{197}\text{Au}$



AGATA-DANTE setup



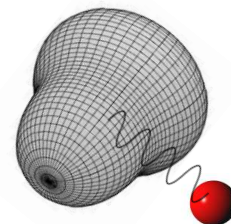
K. Hadyńska *et al.* Phys. Rev. Lett. 117, 062501 (2016)



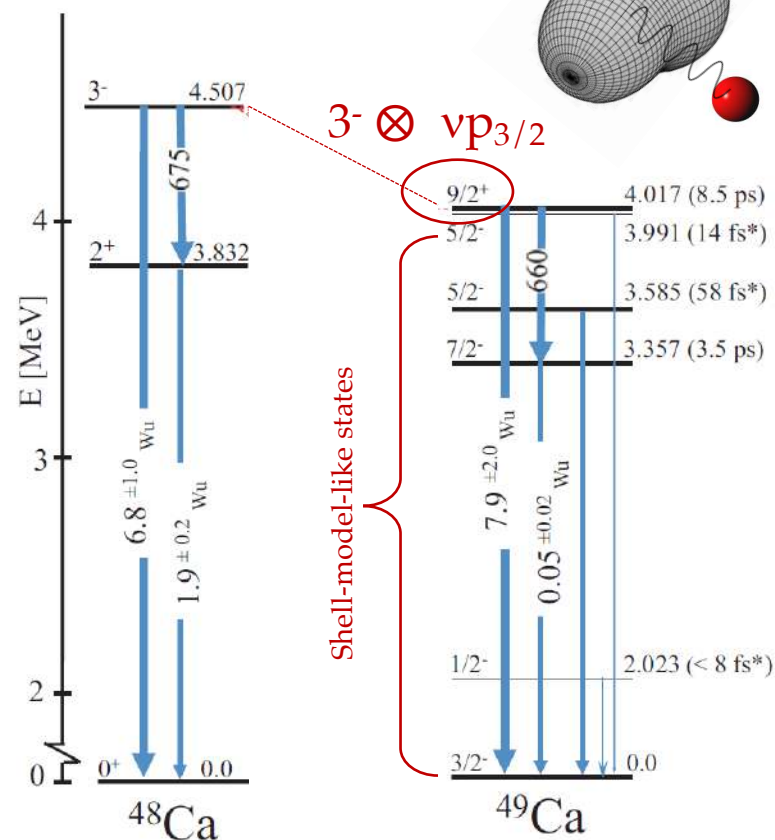
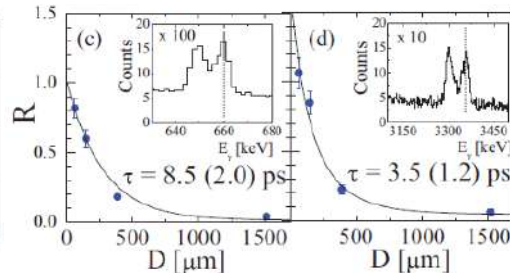
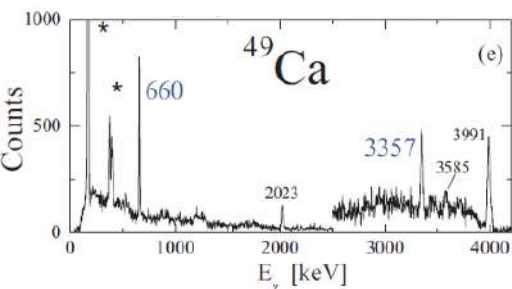
# Ca isotopes: coexistence of complex structures

## PARTICLE-VIBRATION COUPLING IN $^{49}\text{Ca}$

### MULTINUCLEON TRANSFER @ LNL



### $\gamma$ -ray spectroscopy and lifetime measurements



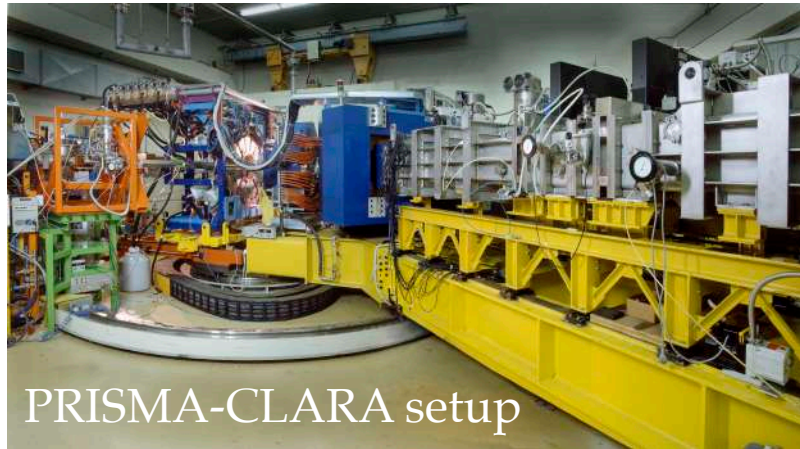
D. Montanari, S. Leoni, D. Mengoni *et al.* Phys. Lett B **697**, 288 (2011)

# Ca isotopes: coexistence of complex structures

## PARTICLE-VIBRATION COUPLING IN $^{47}\text{Ca}$

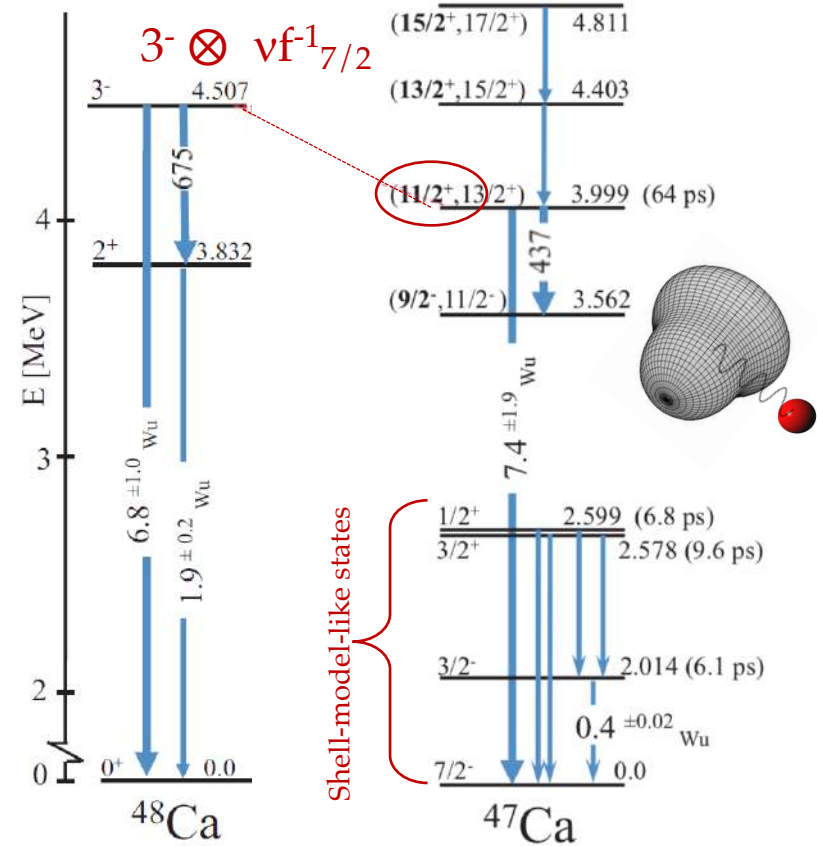
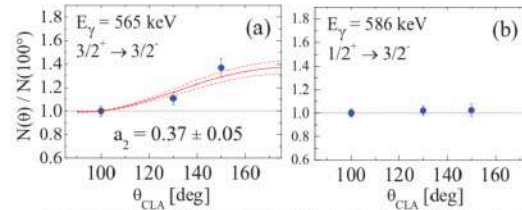
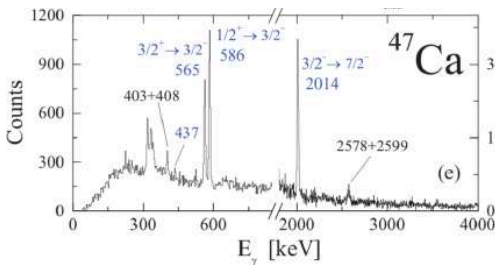
MULTINUCLEON TRANSFER @ LNL

$^{48}\text{Ca} + ^{64}\text{Ni} / ^{208}\text{Pb}$



$$^{47}\text{Ca} = ^{48}\text{Ca} + 1\nu^{-1}$$

$\gamma$ -ray spectroscopy and lifetime measurements

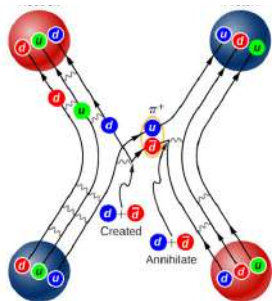


D. Montanari, S. Leoni, D. Mengoni *et al.* Phys. Lett B **697**, 288 (2011)

# Ca isotopes: benchmark for different theories

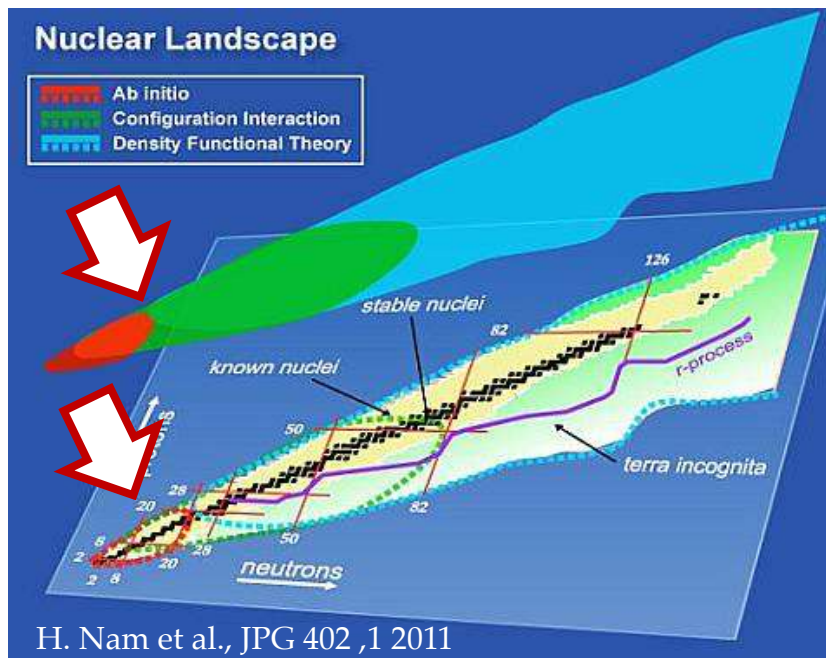
## NEED OF AN UNIFIED DESCRIPTION OF NUCLEAR STRUCTURE

### AB INITIO METHODS

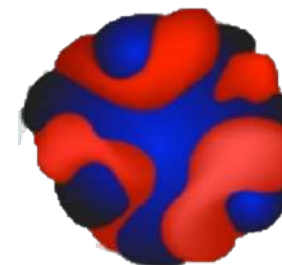


N-N interaction derived from first principles (QCD)

J. D. Holt, J. Menendez, J. Simonis, and A. Schwenk, Phys. Rev. C **90**, 024312 (2014)



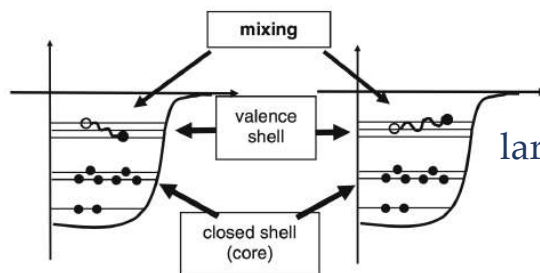
### DENSITY FUNCTIONAL THEORY



Energy Density Functionals based on effective interactions (Skyrme, Gogny, ...)

M. Bender, P.-H. Heenen, P.-G. Reinhard Rev. Mod. Phys. **75**, 121 (2003)

### SHELL MODEL CALCULATIONS



Effective and realistic interactions in large configuration spaces ( $\geq 10^{10}$ )

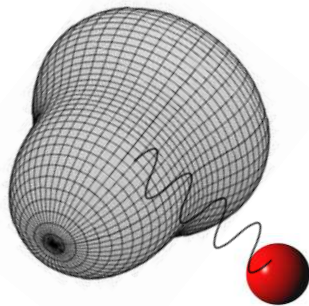
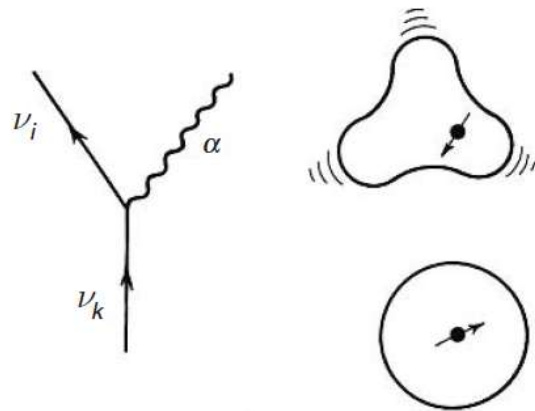
computational challenging

Y. Utsuno, T. Otsuka, B. A. Brown, M. Honma, T. Mizusaki, and N. Shimizu, Progr. Theor. Phys. Suppl. **196**, 304 (2012)



## Nuclear physics

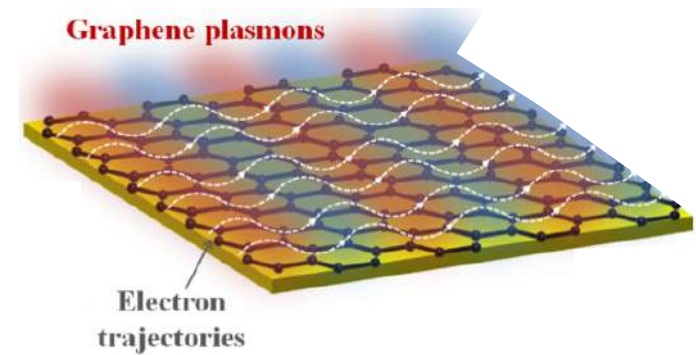
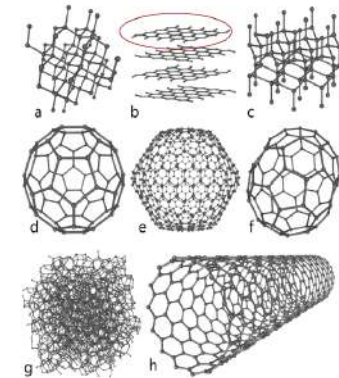
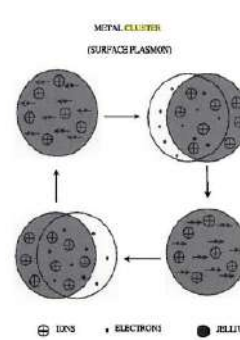
oscillations of the nucleon density



phonon-nucleon couplings

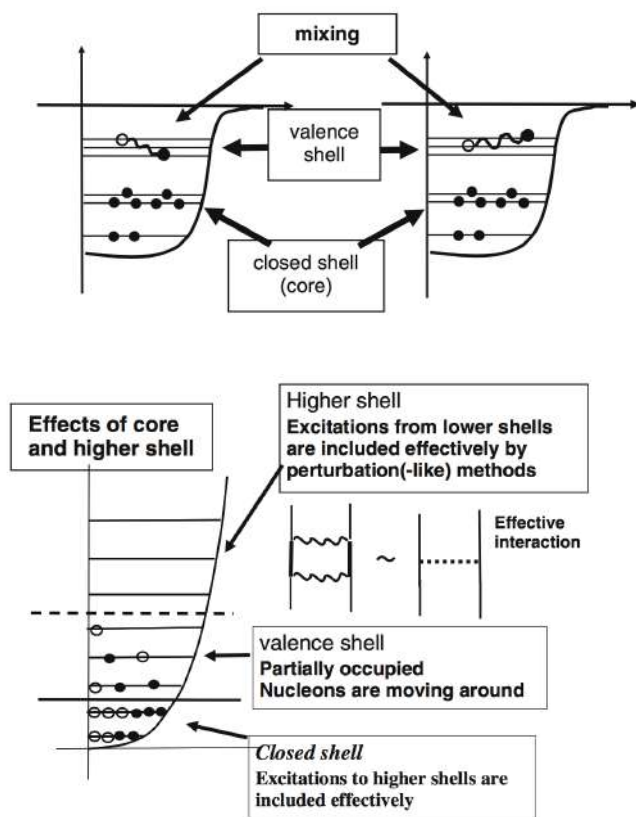
## Solid state physics

oscillations of the free-electron density



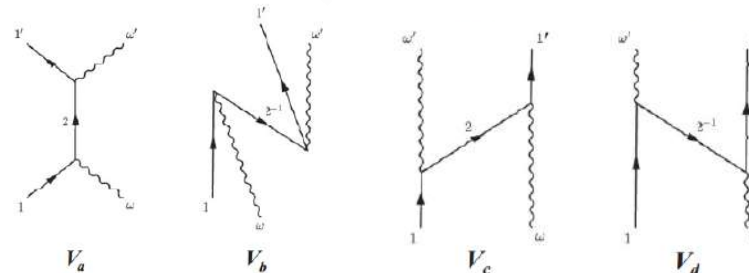
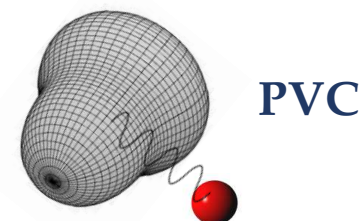
plasmon-electron couplings

## Shell model



from T. Otsuka

## Perturbative Particle-Vibration Coupling



$$\langle [j' \otimes J]_j | V_a + V_b | [j' \otimes J]_j \rangle = \sum_{j_1} \frac{1}{2j_1 + 1} \frac{\langle j_1 || V || j', J \rangle^2}{\varepsilon(j') - \varepsilon(j_1) + \hbar\omega_J}$$

$$\langle [j' \otimes J]_j | V_c + V_d | [j' \otimes J]_j \rangle = \sum_{j_1} \frac{2j' + 1}{2j_1 + 1} \left\{ \begin{matrix} J & j' & j_1 \\ J & j' & j \end{matrix} \right\} \frac{\langle j_1 || V || j', J \rangle^2}{\varepsilon(j_1) - \varepsilon(j') + \hbar\omega_J}$$

from A. Bohr and B. Mottelson

- No collective excitations of the core
- Large increase of configurations involved

- Phenomenological approach
- Weak coupling approximation

## THE HYBRID CONFIGURATION MIXING MODEL (HCM)

### Microscopic model for odd-mass nuclei

G. Colò *et al.*, Phys. Rev. C. **95**, 034303 (2017)

S. Bottoni *et al.*, to be published

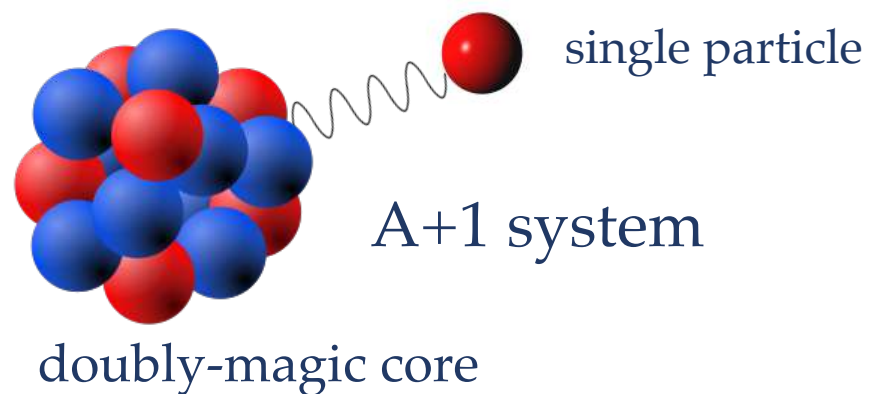
#### SKYRME HAMILTONIAN

$$H = H_0 + V,$$
$$H_0 = \sum_{jm} \varepsilon_j a_{jm}^\dagger a_{jm} + \sum_{NJM} \hbar\omega_{NJ} \Gamma_{NJM}^\dagger \Gamma_{NJM},$$
$$V = \sum_{jmj'm'} \sum_{NJM} h(jm; j'm', NJM) a_{jm} [a_{j'}^\dagger \otimes \Gamma_{NJ}^\dagger]_{jm}$$

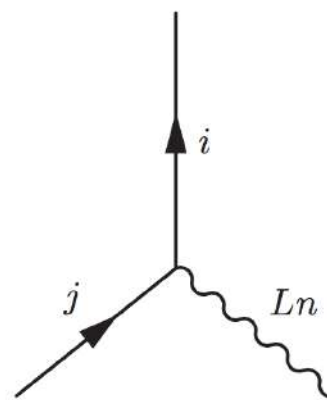
#### BASIS

Single-particle/hole states (Hartree-Fock)

Collective phonons and  
non collective 1p-1h excitations  
(Random Phase Approximation)



#### COUPLING VERTEX



G. Colò, H. Sagawa and P.F. Bortignon  
Phys. Rev. C **82**, 054307 (2010)

# The experimental campaign at Institut Laue-Langevin Grenoble (France)



*www.ill.eu*



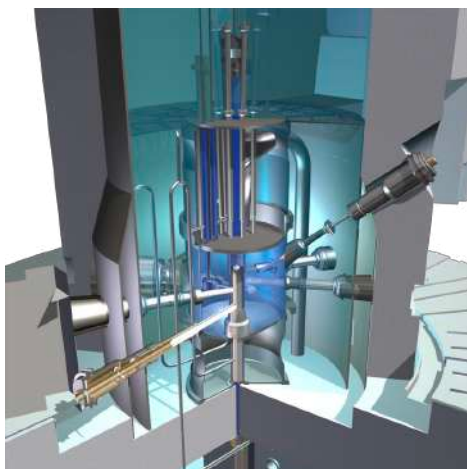
# The Institut Laue-Langevin (ILL)

## HIGH FLUX REACTOR

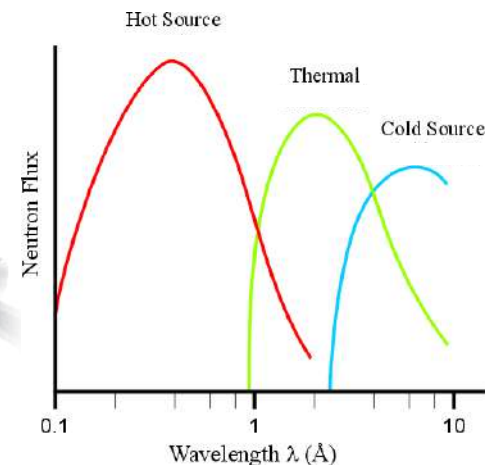
$1.5 \cdot 10^{15}$  neutrons/s/cm<sup>2</sup>  
(continuous beams)

Thermal Power  
58.3 MW

50-day cycles

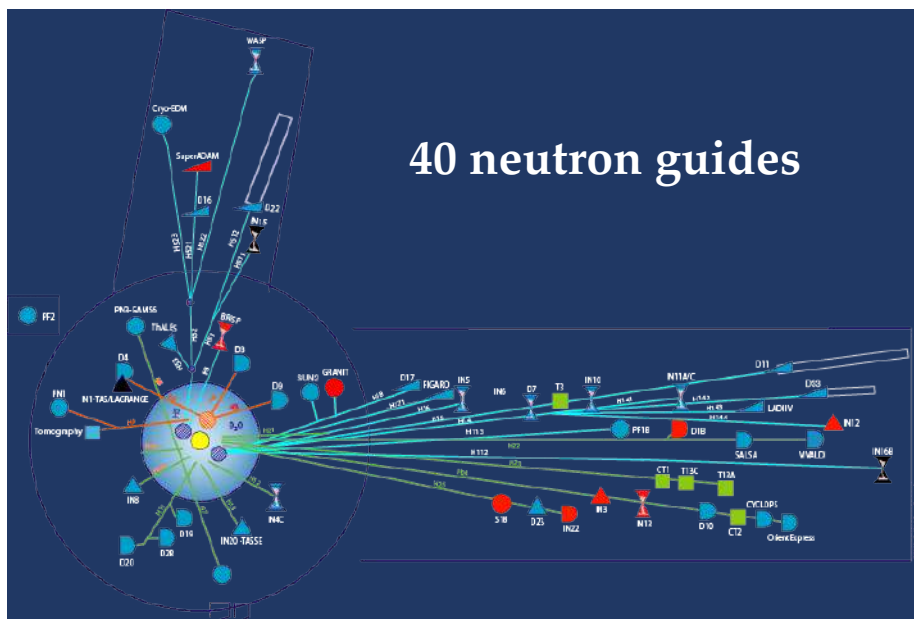


## NEUTRONS AT ILL



## EXPERIMENTS AT ILL

40 neutron guides



**FUNDAMENTAL SCIENCE:**

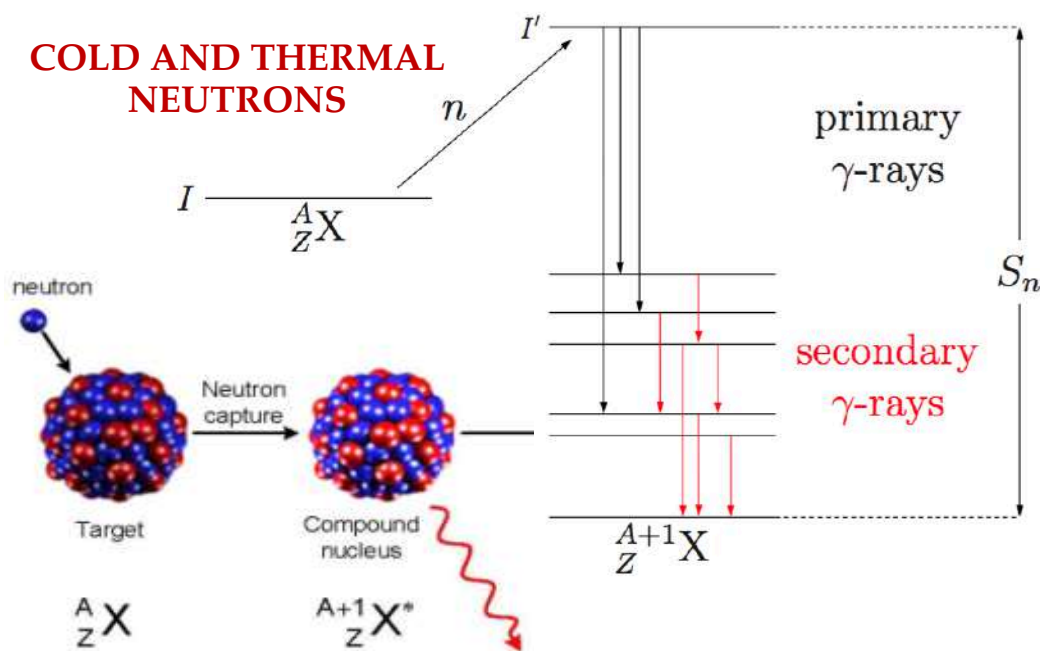
Condensed matter physics

Material Science

Chemistry and Biology

**Nuclear and Particle physics**

## NEUTRON-CAPTURE REACTIONS



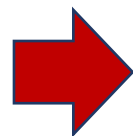
$$J_{I'} = J_I \pm 1/2$$

$$n + X = (X + 1)$$

$$\underbrace{T_n}_{\text{meV}} + \underbrace{m_n c^2}_{\text{GeV}} + \underbrace{m_X c^2}_{\text{GeV}} = \underbrace{m_{X+1} c^2}_{\text{GeV}} + \underbrace{T_{X+1}}_{\ll \text{meV}} + \underbrace{E_{X+1}^*}_{\text{MeV}}$$

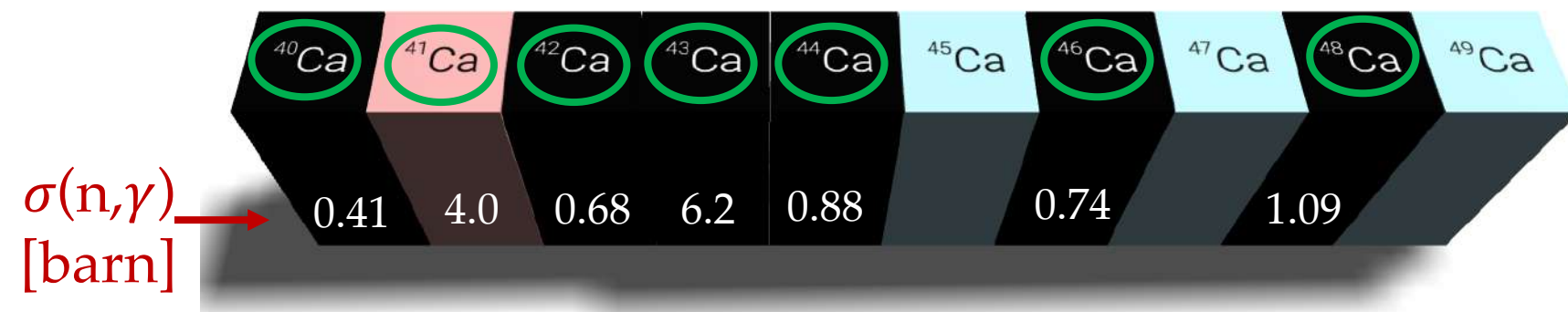
$$E_{X+1}^* = (m_n c^2 + m_X c^2) - m_{X+1} c^2 \equiv S_n$$

Complete low-spin  $\gamma$ -ray spectroscopy from the capture state to the ground state



Complementary to higher-spin spectroscopy with stable and radioactive beams

## RARE AND RADIOACTIVE TARGETS



### <sup>41</sup>Ca

CaCO<sub>3</sub>

A ~ 2 MBq

m ~ 600 μg

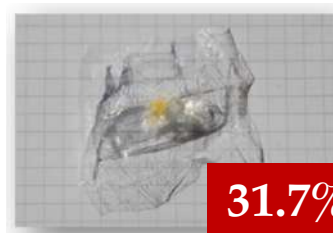
63.4%

$t_{1/2} \sim 10^5$  y

made in 1975



### <sup>46</sup>Ca



31.7%

Ca(NO<sub>3</sub>)<sub>2</sub>  
(40.6 mg)

Abundance  
0.004%

made at PSI by A. Türler

### <sup>48</sup>Ca

60.5%

CaCO<sub>3</sub>  
(350 mg)

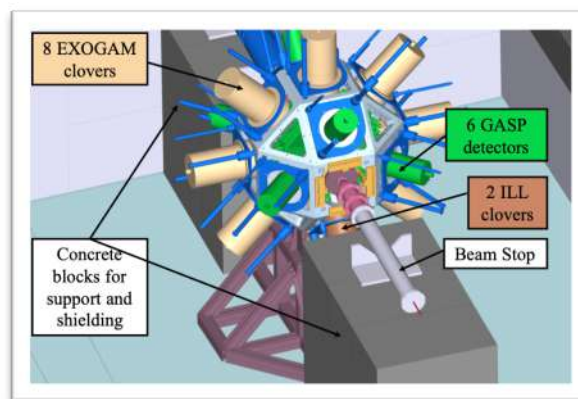
Abundance  
0.187%

made in 1979

# Experimental program at ILL

## THE EXILL CAMPAIGN (2012-2013)

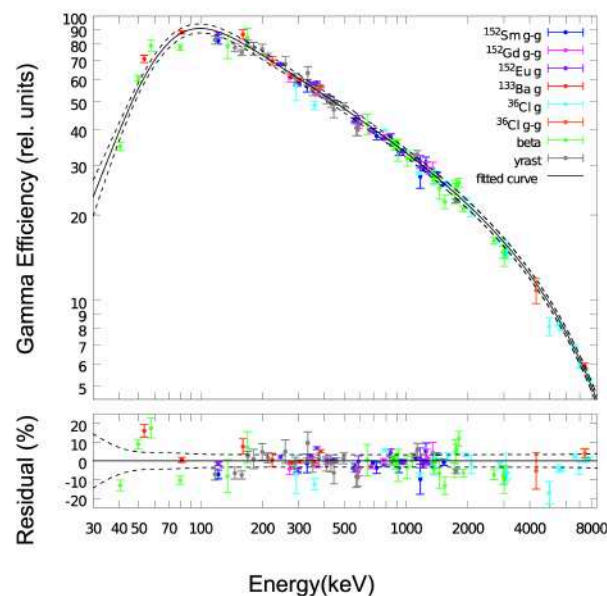
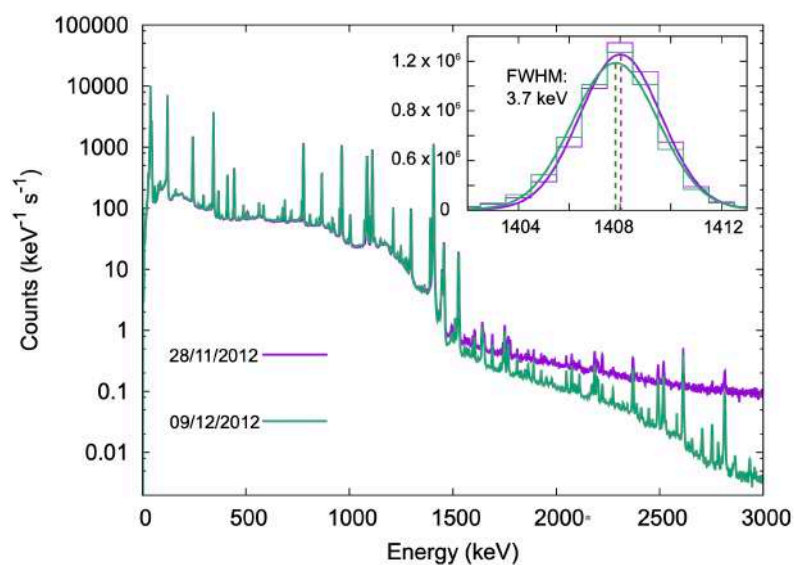
Promoted by W. Urban –  $^{48}\text{Ca}(n,\gamma)$  first measurement



First campaign with a large  $\gamma$  array and a neutron beam (cold neutrons)

HPGe detectors

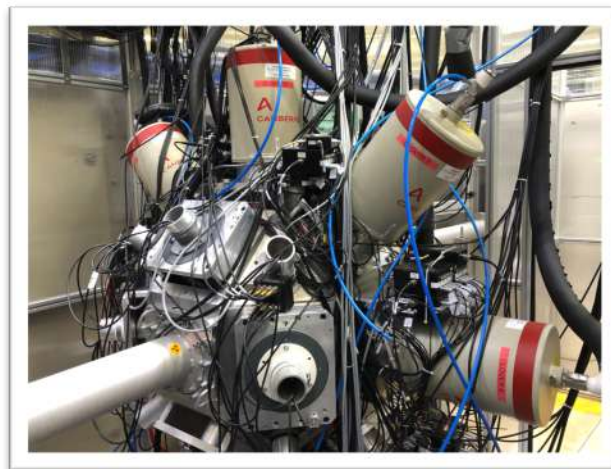
LaBr:Ce scintillators



M. Jentschel *et al.*, J. Inst. 12, 11003 (2017)



## THE FIPPS PERMANENT SETUP (SINCE 2016)

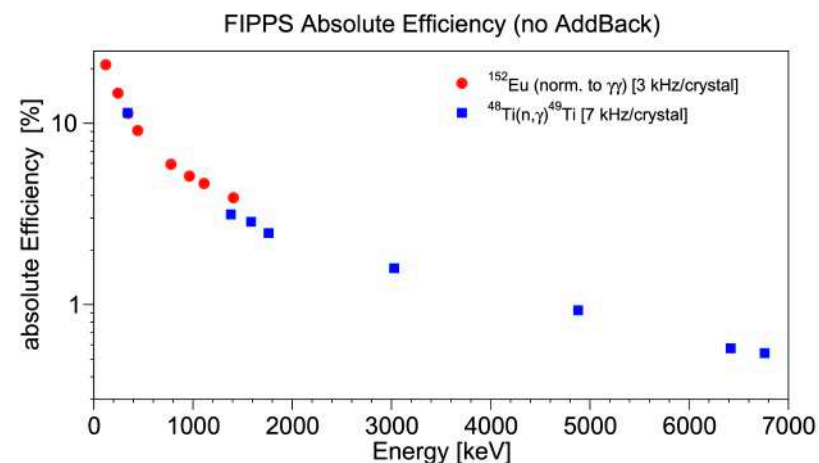
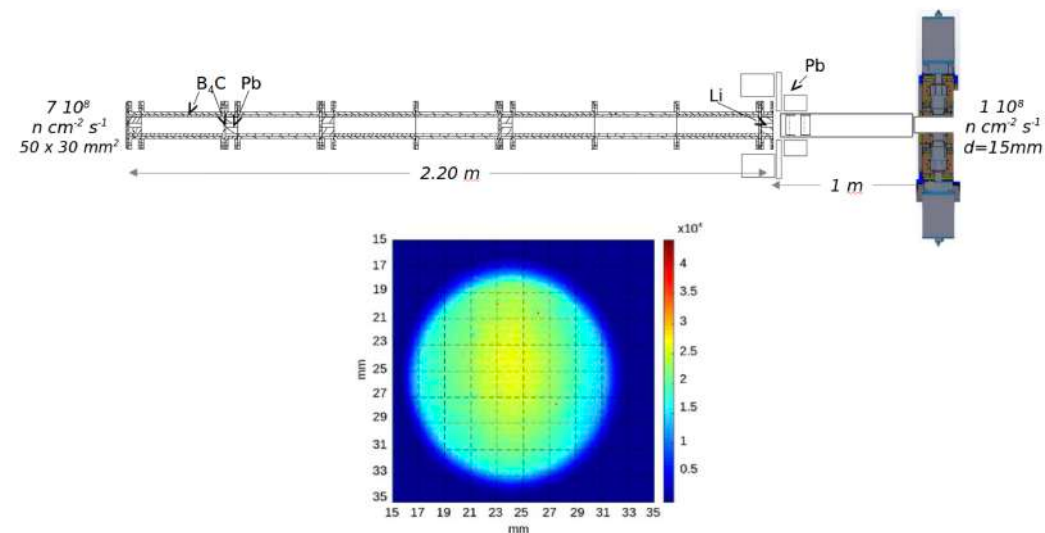


thermal neutrons

HPGe clover detectors + AC shields

Clover detectors from IFIN-HH  
(Bucharest)

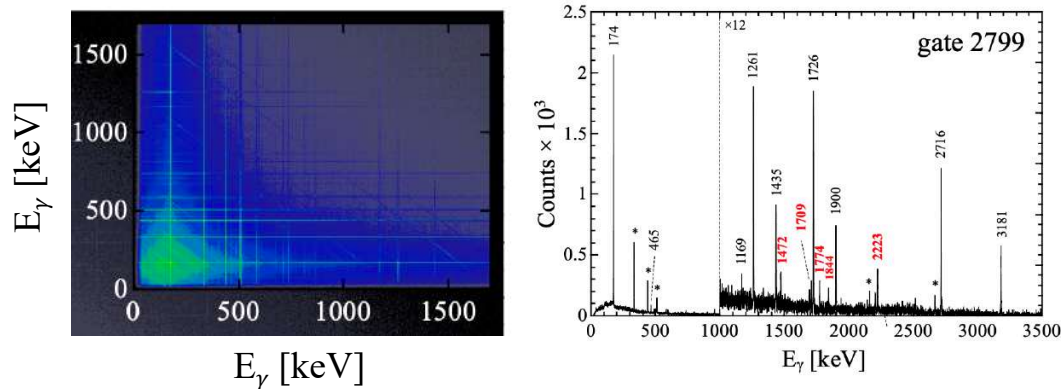
LaBr:Ce scintillators



C. Michelagnoli *et al.*, EPJ 193, 04009 (2018)

## EXPERIMENTAL TECHNIQUES

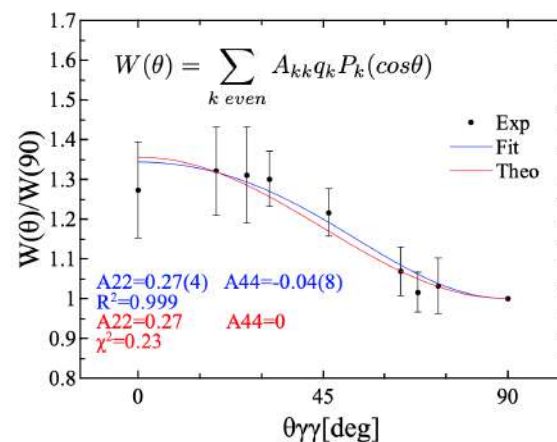
### High-resolution $\gamma$ -ray spectroscopy



$\gamma$ - $\gamma$  coincidences  
Prompt-Delay correlations  
Level and decay schemes  
 $\gamma$ -ray intensities

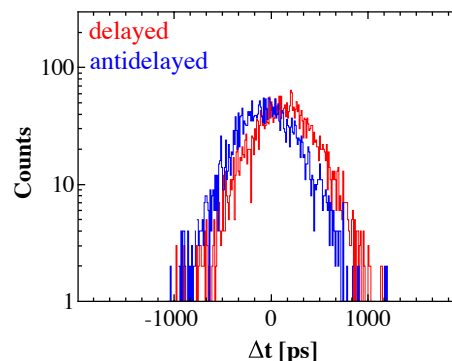
 Information on  
state wave function

### Angular correlations



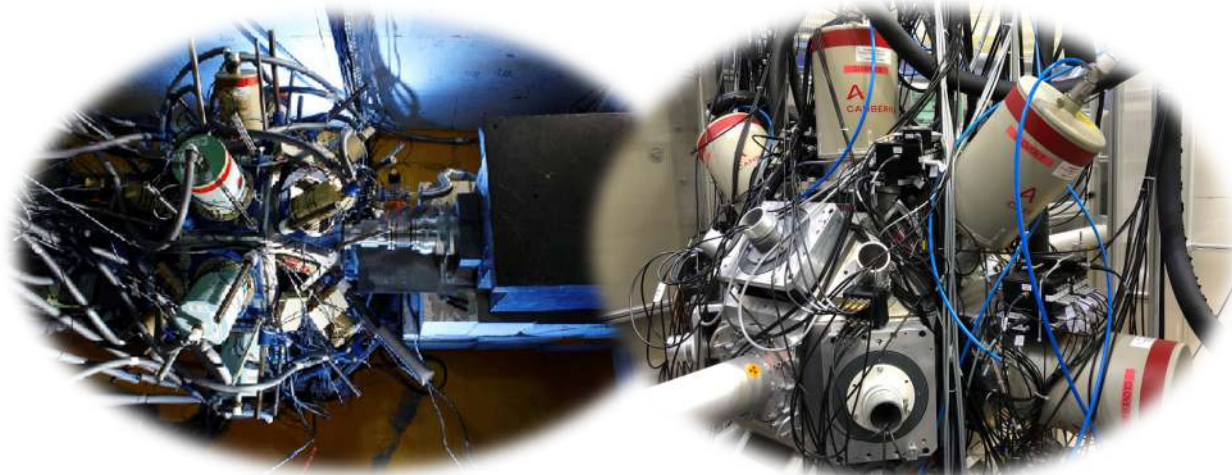
$\gamma$ -ray multipolarities  
Spin assignments

### Lifetime measurements



LaBr:Ce detectors  
Fast-timing techniques  
Picosecond range

# Recent results



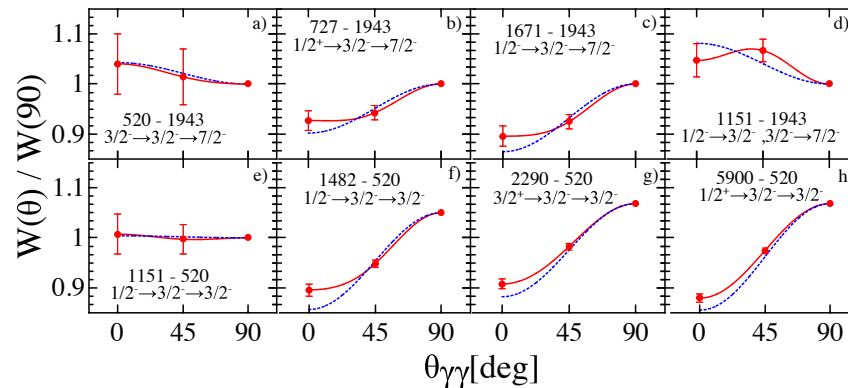
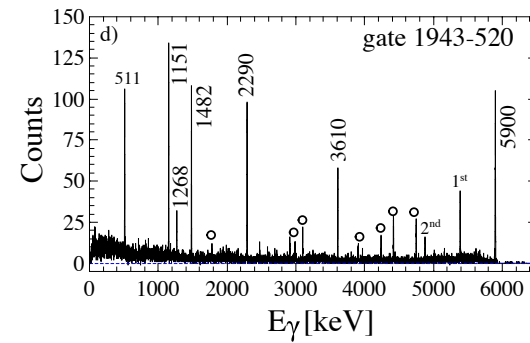
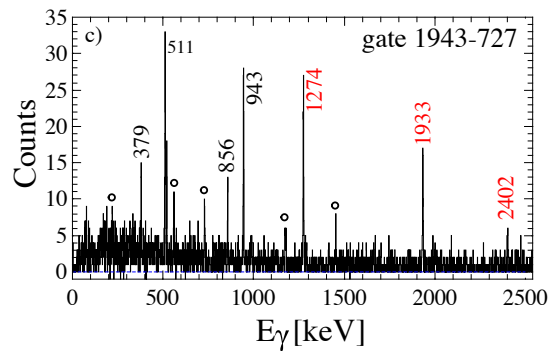
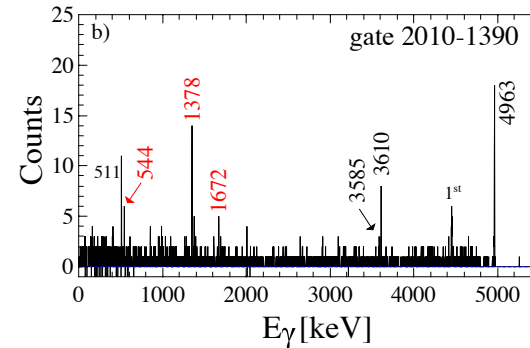
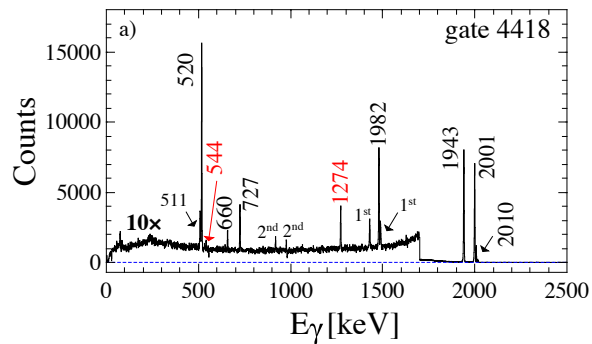
**EXILL**

**FIPPS**

PHYSICAL REVIEW C **103**, 014320 (2021)

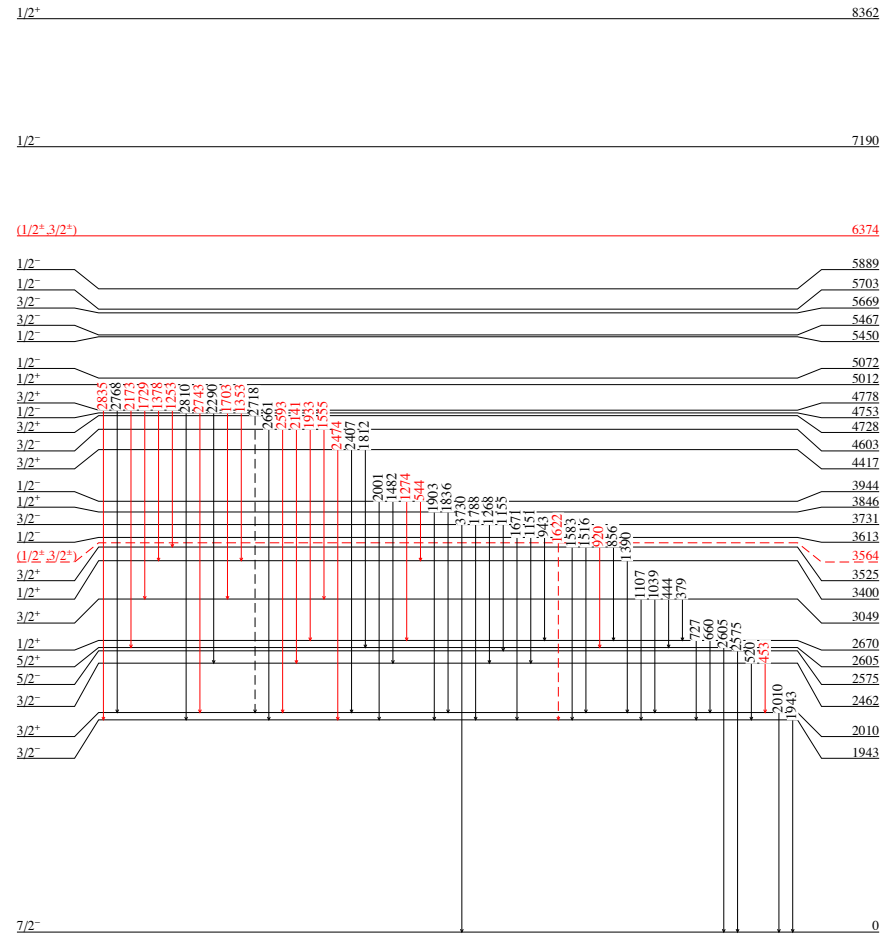
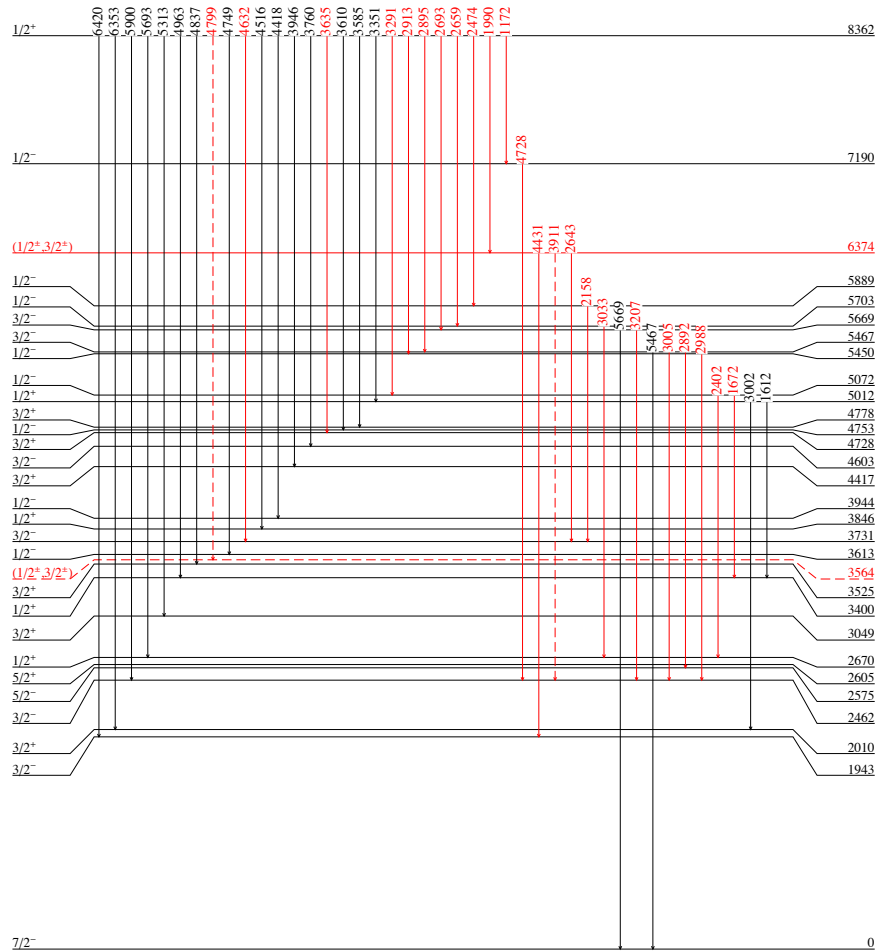
**Low-spin particle-core and hole-core excitations in  $^{41,47,49}\text{Ca}$  isotopes studied by cold-neutron-capture reactions**

S. Bottoni<sup>1,2,\*</sup> N. Cieplicka-Oryńczak<sup>3</sup> S. Leoni<sup>1,2</sup> B. Fornal<sup>3</sup> G. Colò<sup>1,2</sup> P. F. Bortignon<sup>1,2</sup> G. Bocchi<sup>1,2</sup>  
D. Bazzacco<sup>4</sup> G. Benzoni<sup>2</sup> A. Blanc<sup>5</sup> A. Bracco<sup>1,2</sup> S. Ceruti<sup>1,2</sup> F. C. L. Crespi<sup>1,2</sup> G. de France<sup>6</sup> E. R. Gamba<sup>7,2</sup>  
Ł. W. Iskra<sup>2,3</sup> M. Jentschel<sup>5</sup> U. Köster<sup>5</sup> C. Michelagnoli<sup>5</sup> B. Million<sup>2</sup> D. Mengoni<sup>8,4</sup> P. Mutti<sup>5</sup> Y. Niu<sup>9</sup>  
C. Porzio<sup>1,2</sup> G. Simpson<sup>5</sup> T. Soldner<sup>5</sup> B. Szpak<sup>3</sup> A. Türler<sup>10</sup> C. A. Ur<sup>11</sup> and W. Urban<sup>12</sup>

$^{41}\text{Ca}$ 



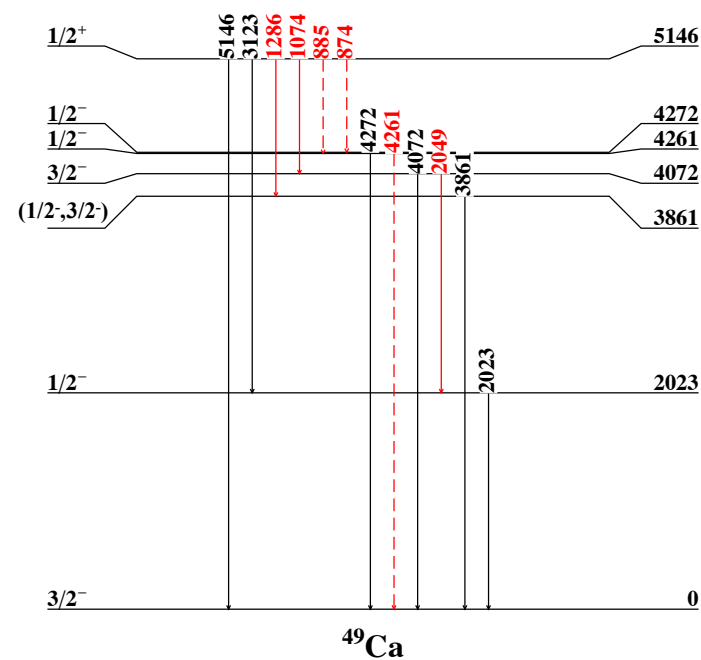
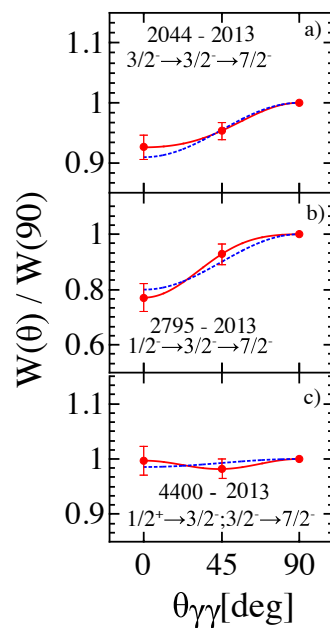
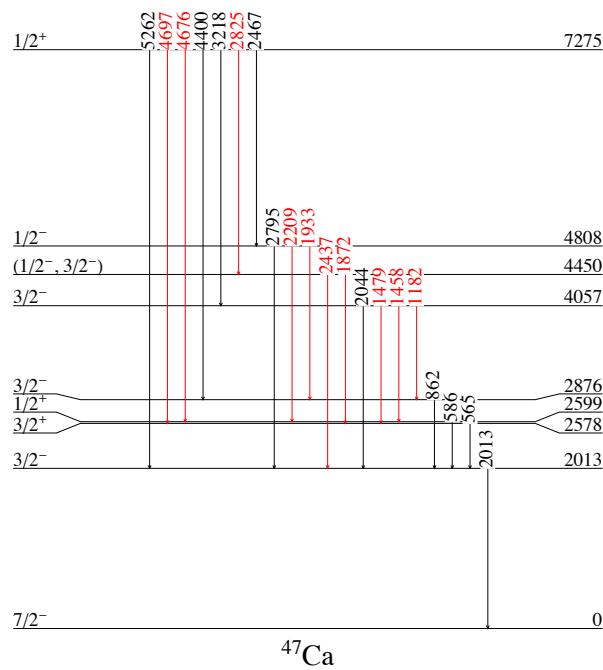
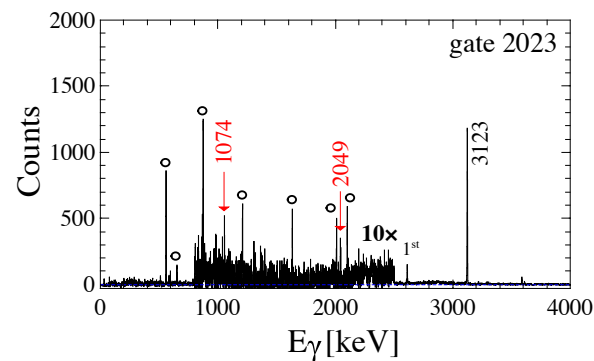
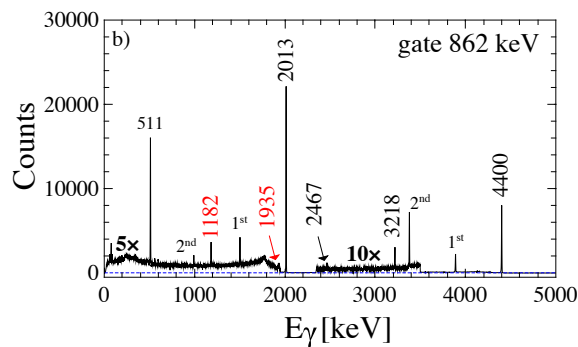
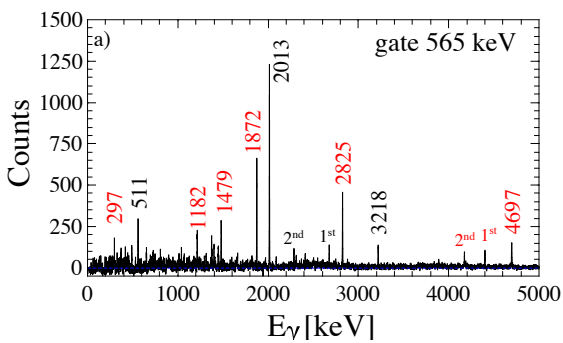
# $^{41}\text{Ca}$



➔ 41 new transitions

# $^{47}\text{Ca}$

# $^{49}\text{Ca}$

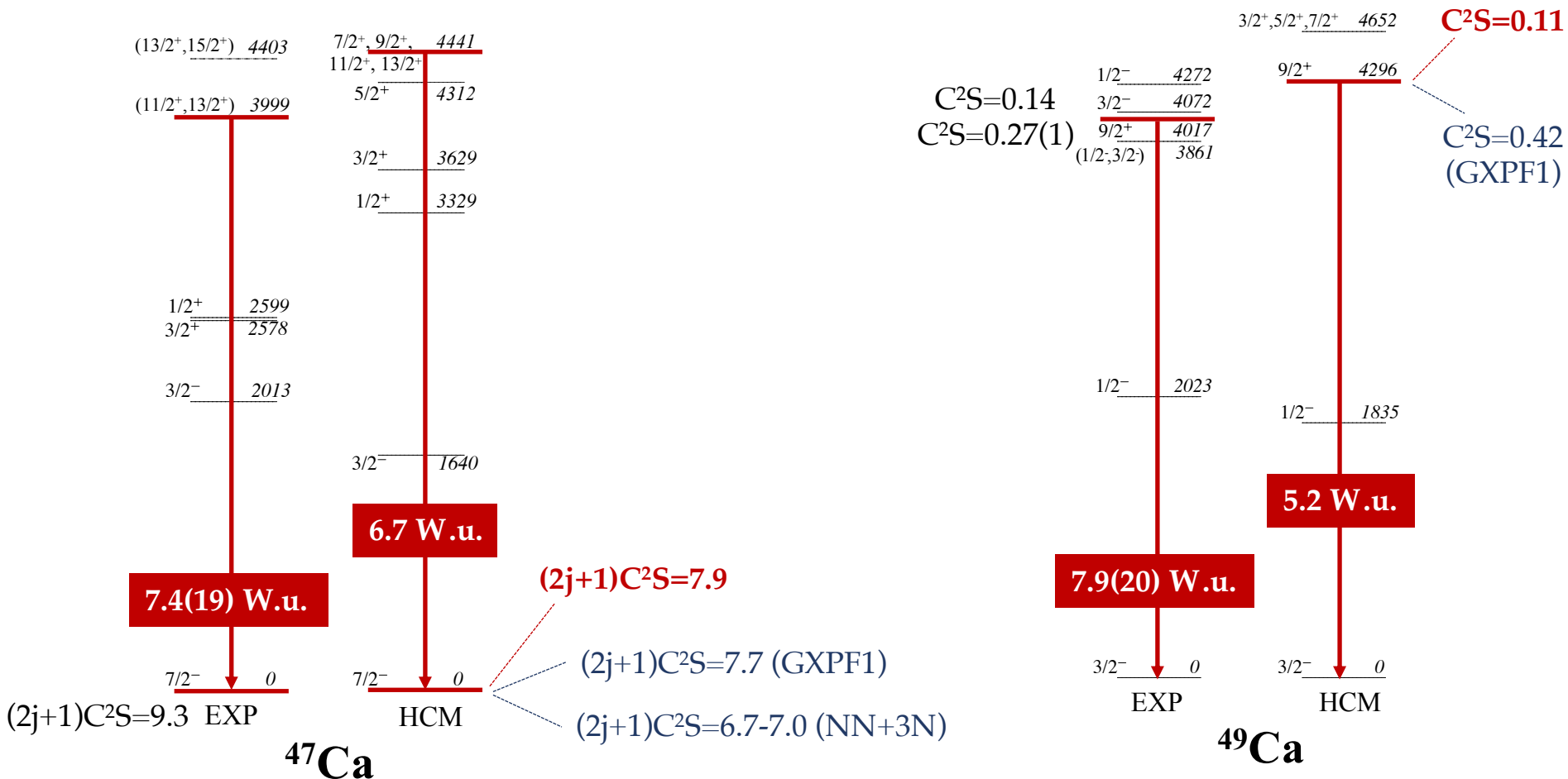




# Comparison with HCM model

$$^{47}\text{Ca} = ^{48}\text{Ca} + 1\nu^{-1}$$

$$^{49}\text{Ca} = ^{48}\text{Ca} + 1\nu$$



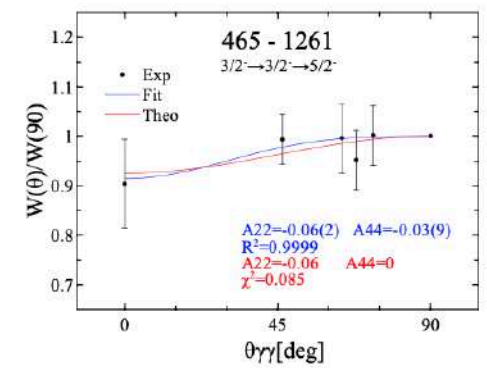
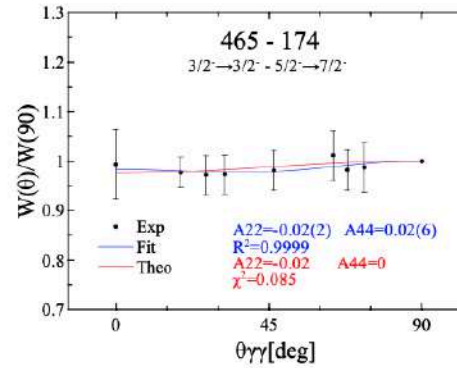
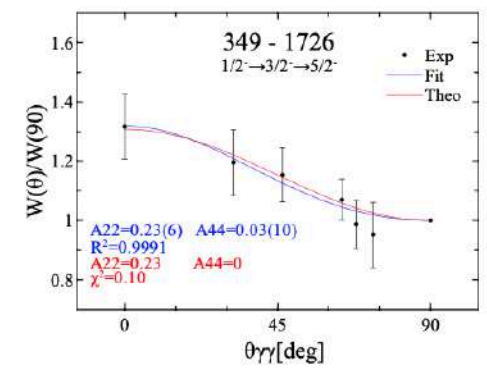
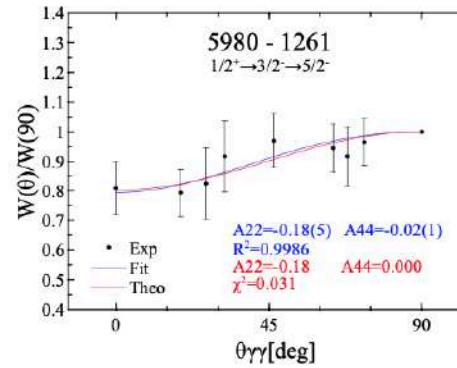
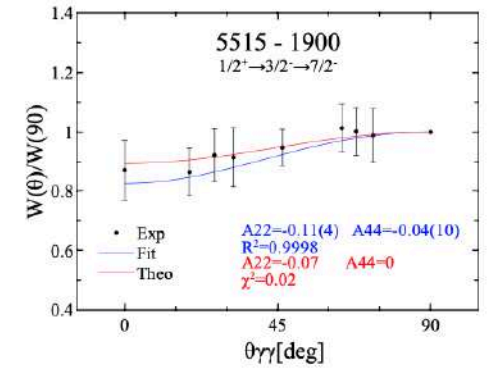
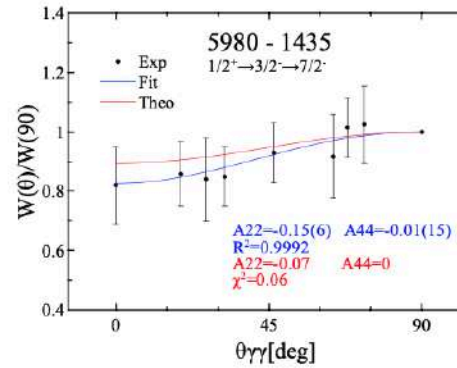
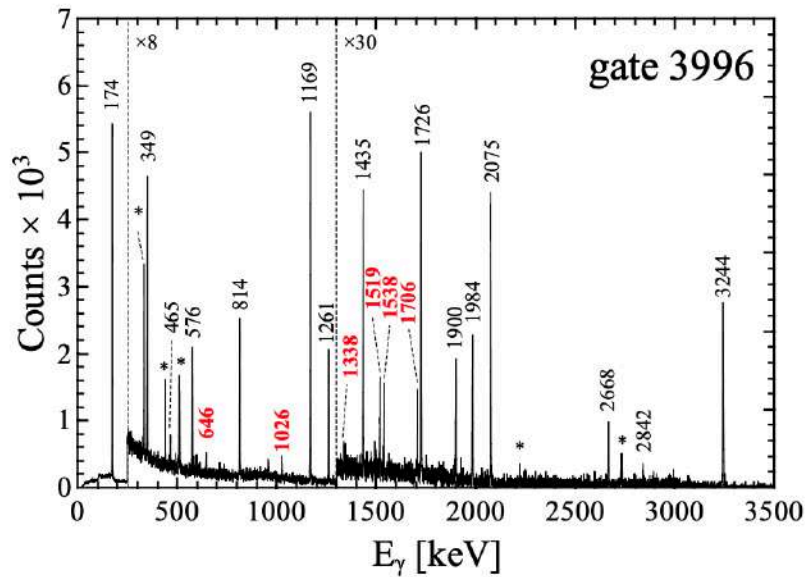
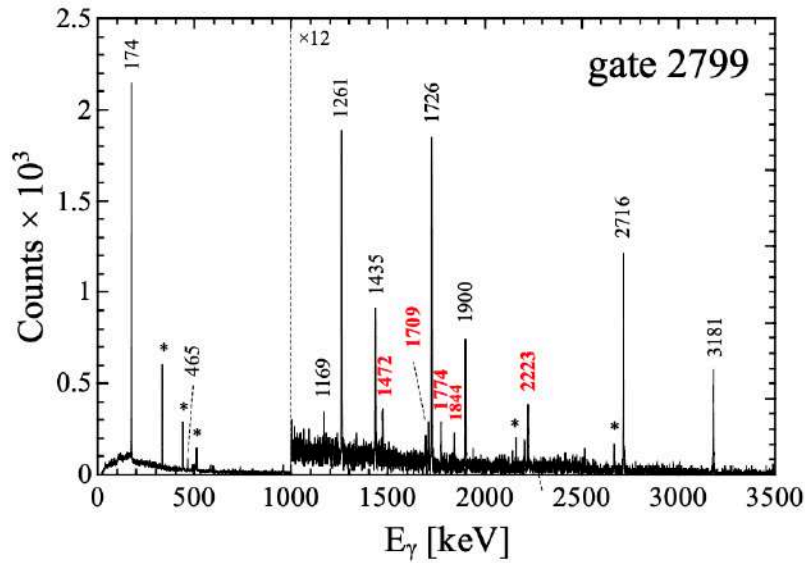
H. L. Crawford et al.,  
PRC 95, 064317 (2017)

Y. Utsuno, et al, Progr. Theor. Phys. Suppl. **196**, 304 (2012)

J. D. Holt, et al, Phys. Rev. C **90**, 024312 (2014)

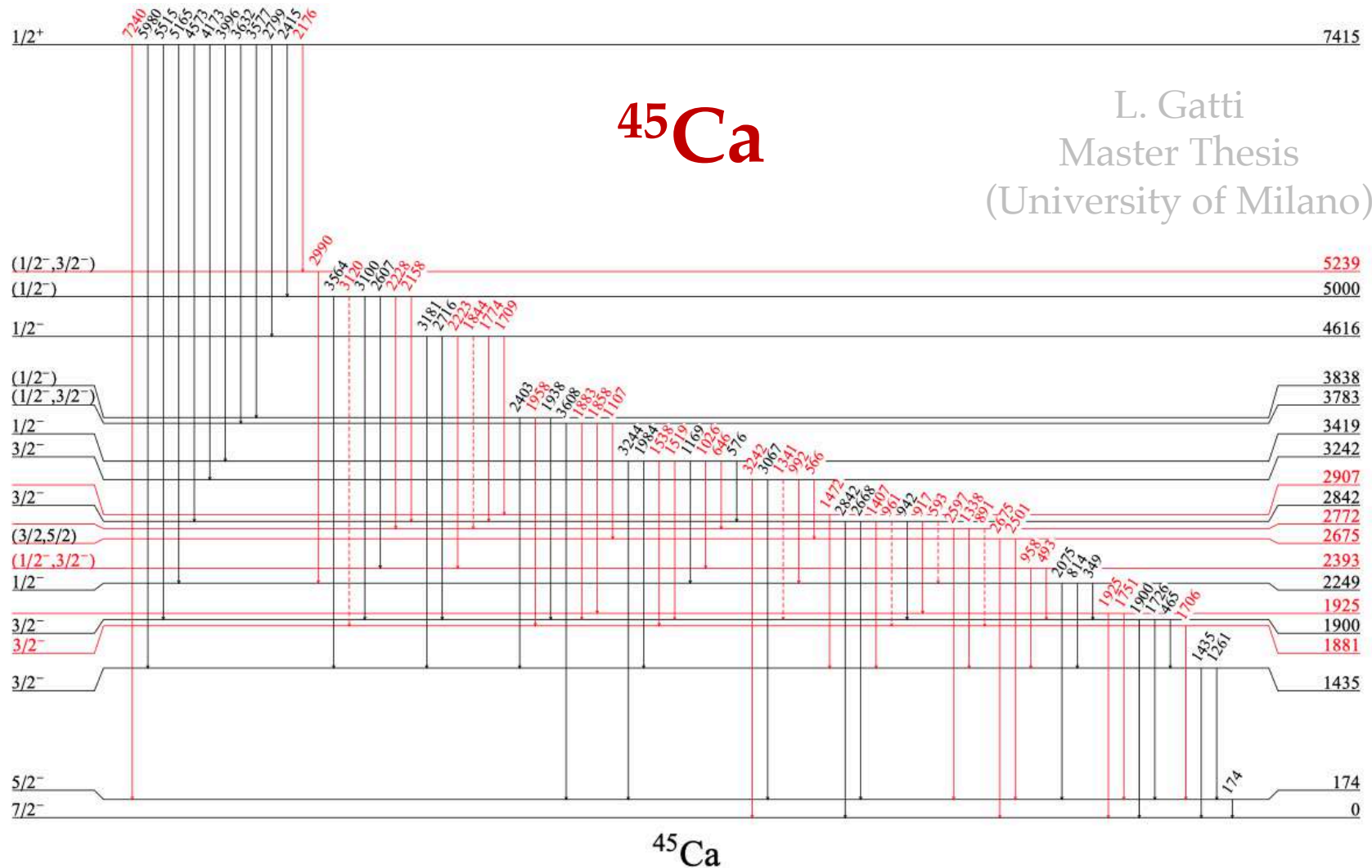
A. Gade et al.,  
PRC 93, 031601(R) (2016)



$^{45}\text{Ca}$ 

## OPEN SHELL NUCLEUS – SUPERFLUID PROPERTIES

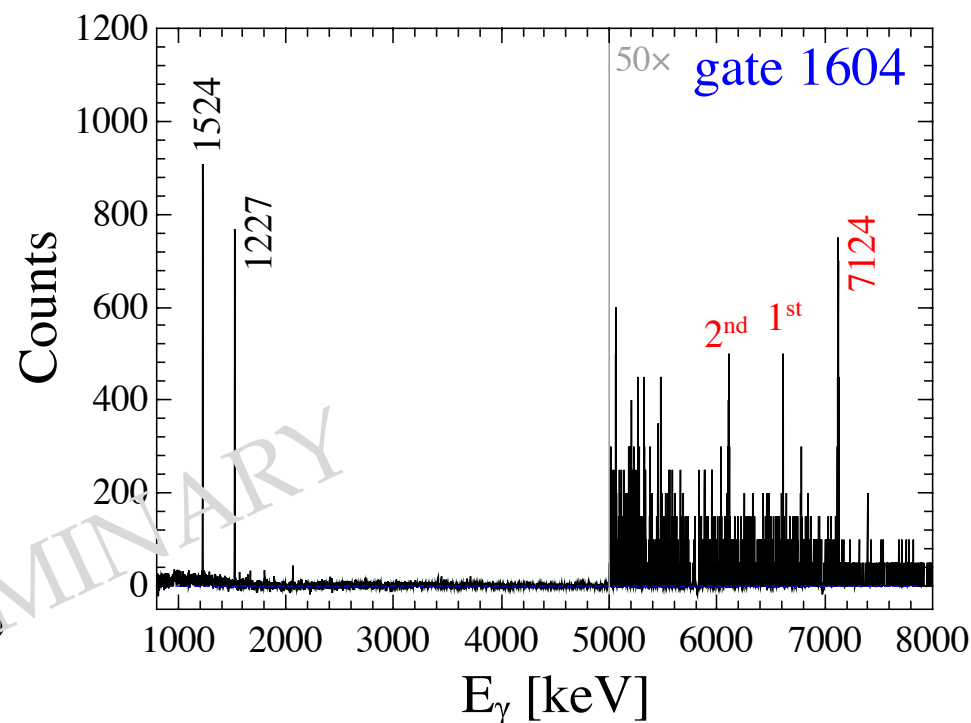
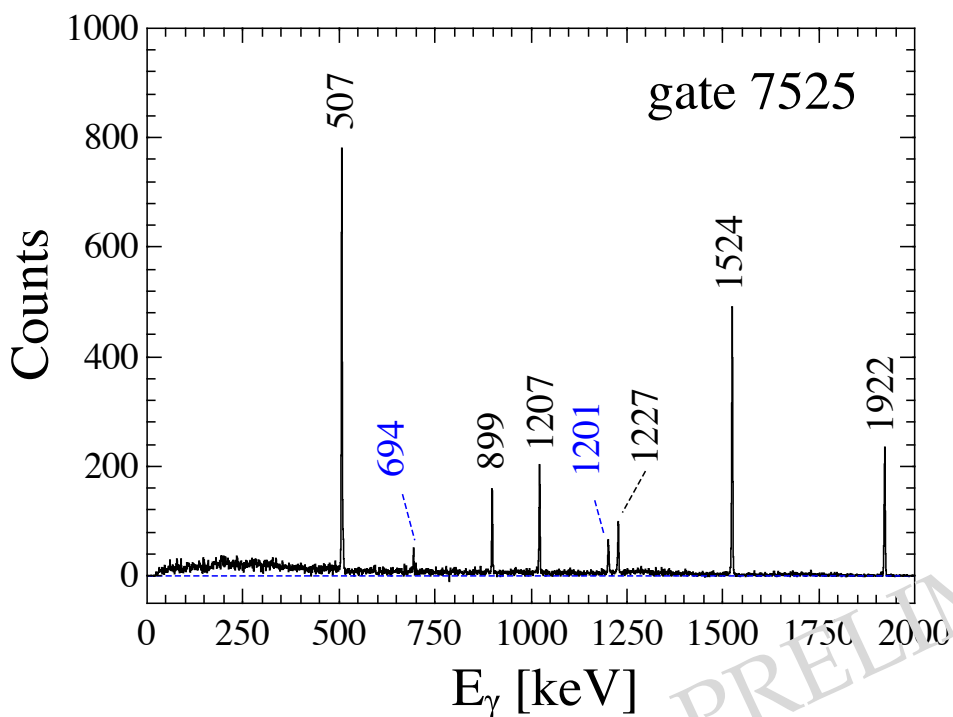
Extension of the HCM model within quasi-particle formalism (Y. Niu)



good statistics and selectivity  
already after 4 hours

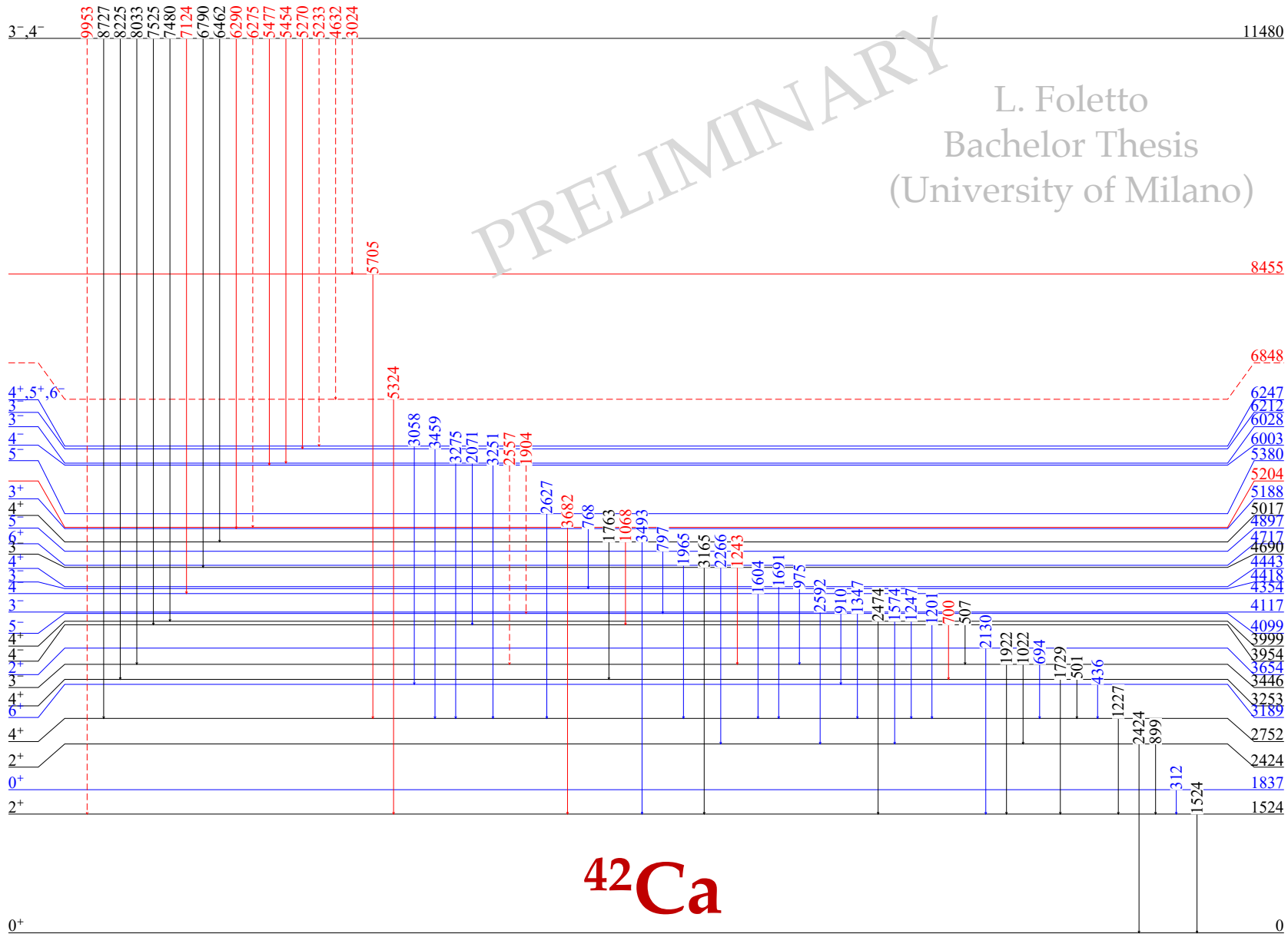


K. Hadyńska *et al.*  
Phys. Rev. Lett. **117**, 062501 (2016)



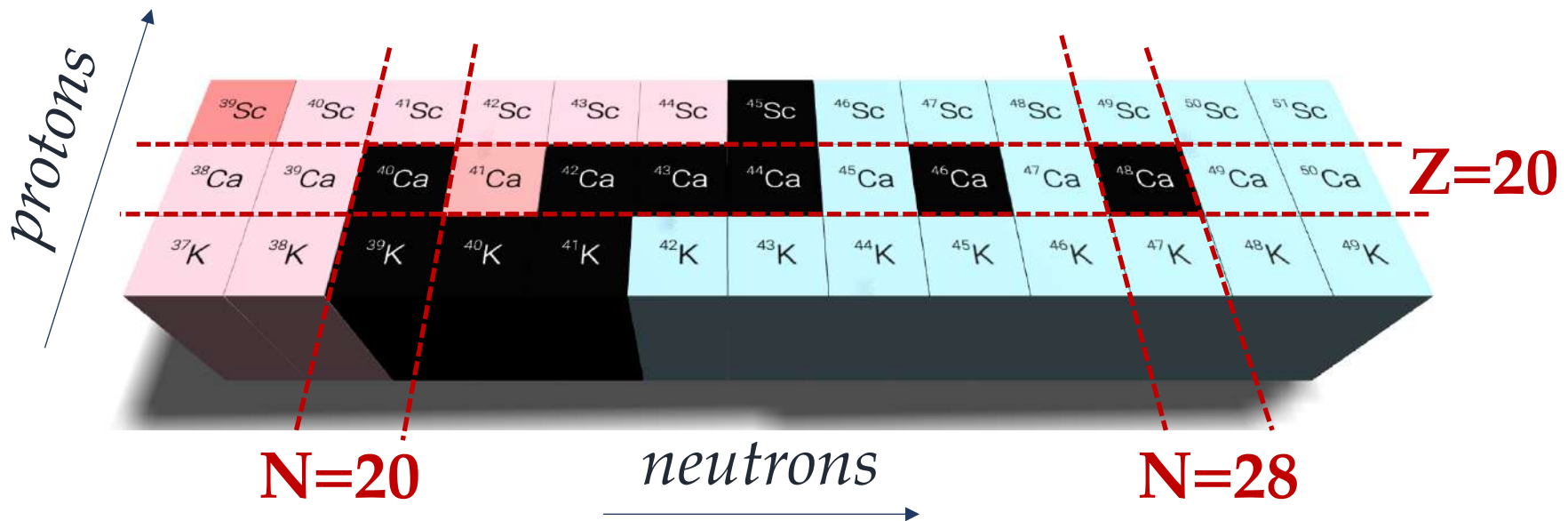
$^{42}\text{Ca}$

# $^{41}\text{Ca}(n,\gamma)^{42}\text{Ca}$ - FIPPS





# Conclusions and future perspectives



# Conclusions and future perspectives

Evolution of **complex structures** along Ca isotopes

**Microscopic origin** of nuclear deformations and core-coupled states

Important **benchmark** for different theory approaches:

from state-of-the-art large-scale **shell-model** calculations to newly-developed models (**Hybrid model**) which allow to reach heavier mass regions



Extensive experimental campaign at **Institut Laue-Langevin**

**Neutron-capture** reactions with **rare and radioactive** targets

High-resolution  **$\gamma$ -ray spectroscopy** and **lifetime** measurements

Importance of **complementary experimental approaches** to reach a complete picture of the complex world of nuclear structure

*Thank you for your attention*

**Simone Bottoni**

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