

# The nuclear charge radius of $^{26m}\text{Al}$ and its implication for $V_{ud}$ in the quark mixing matrix

UW Nuclear Physics Seminar

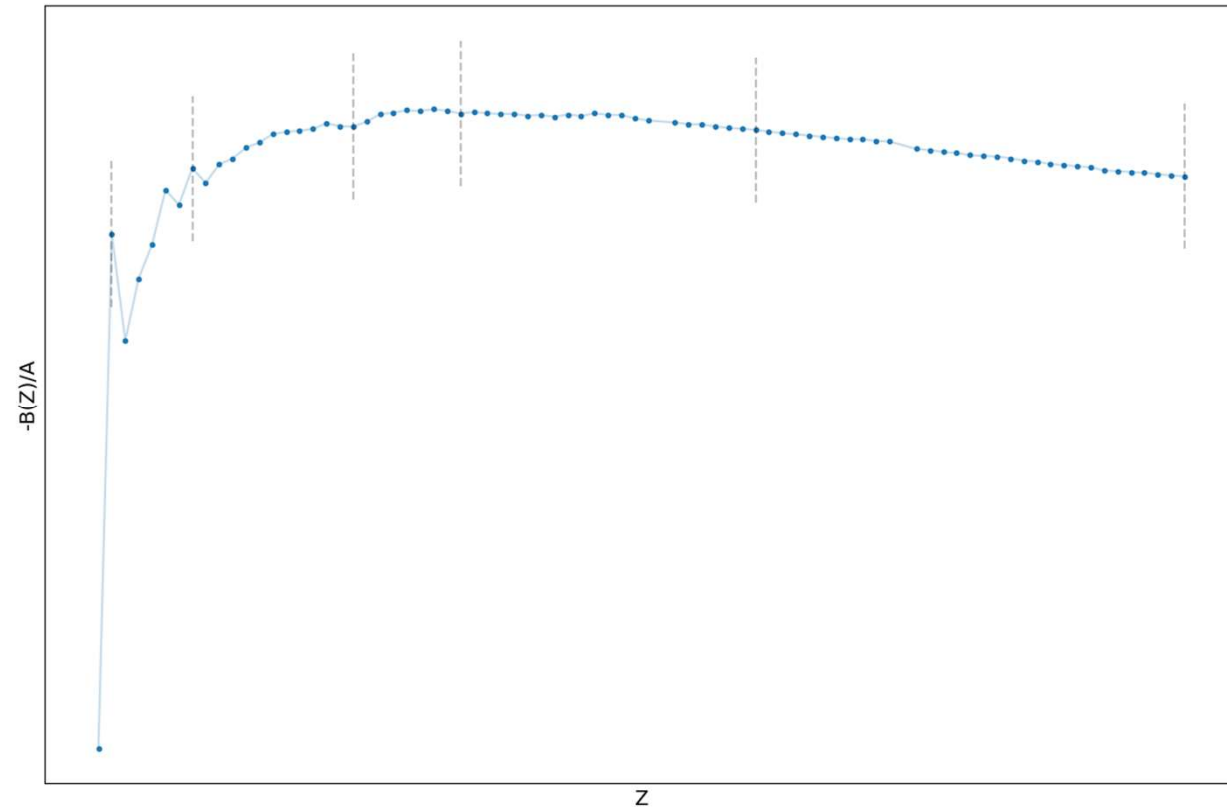
Peter Plattner

# Outline

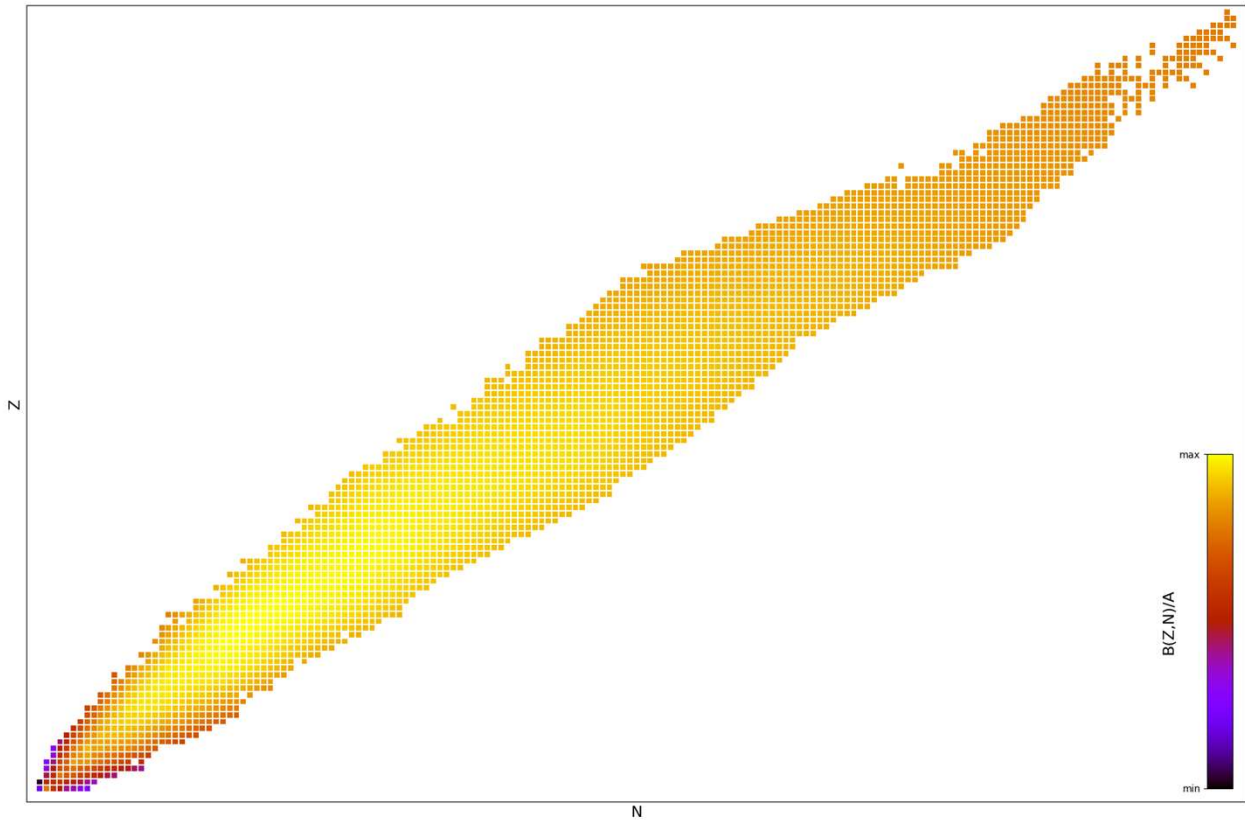
- Motivation
- Determination of  $V_{ud}$
- Introduction to laser spectroscopy and isotope production
- Results of measurements
- Outlook and conclusion

# Binding Energy

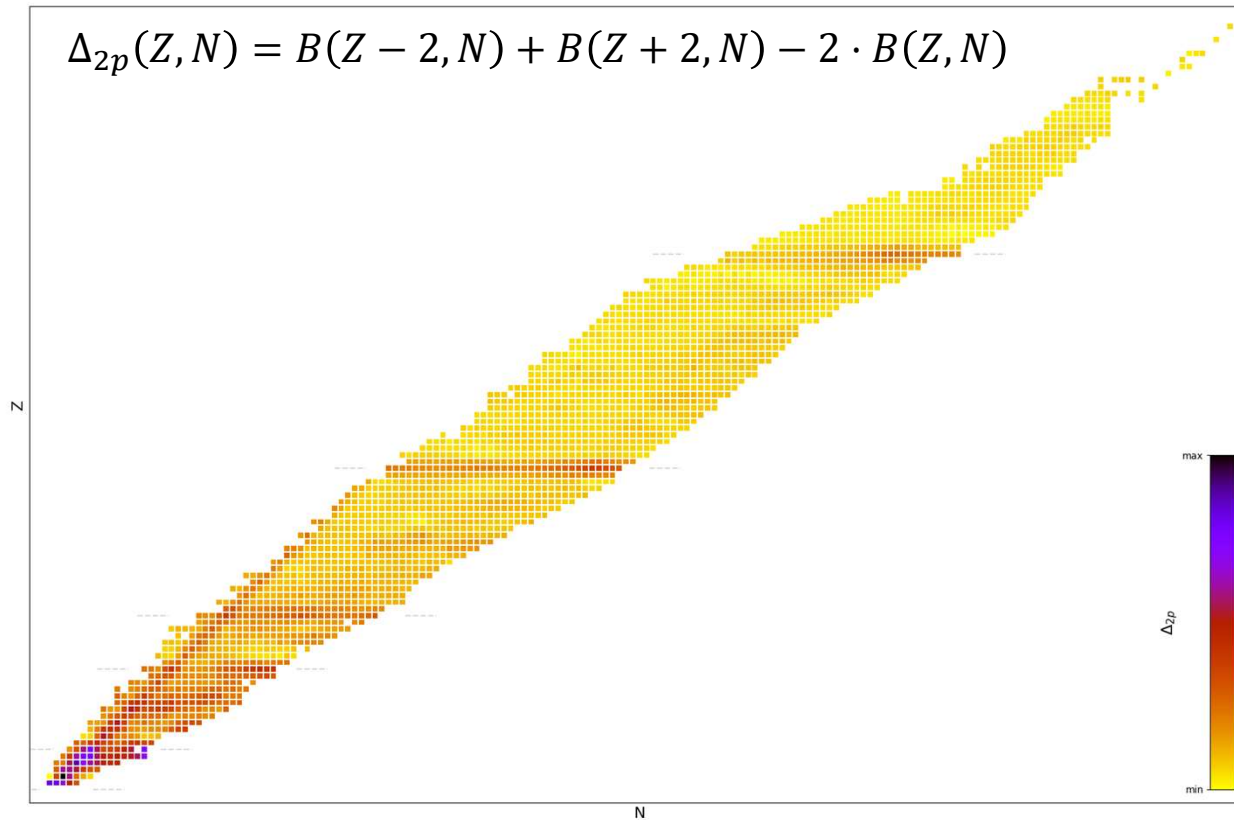
- Binding energy per nucleon for most abundant stable isotopes of each element
- Certain elements show enhanced stability compared to immediate neighbours



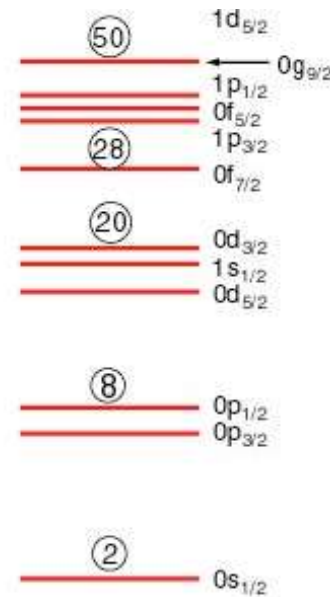
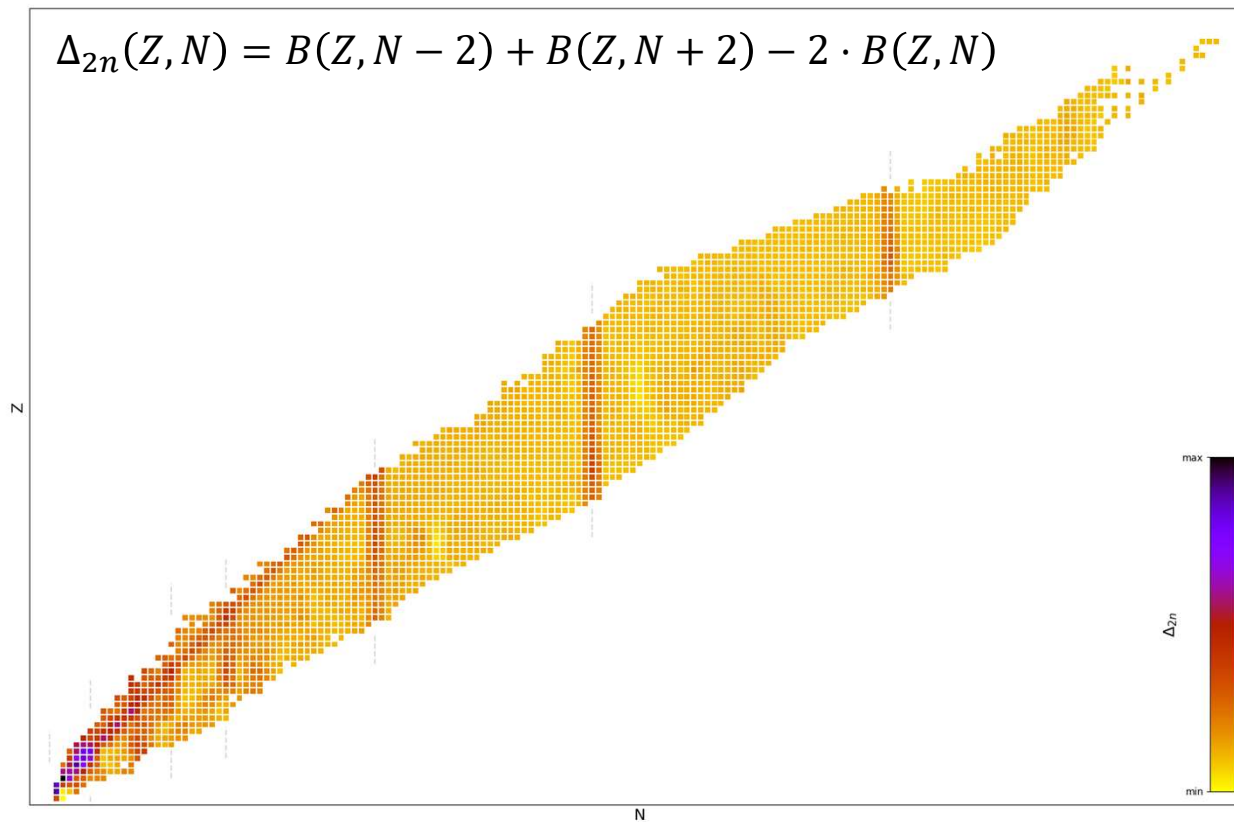
# Binding Energy over Nuclear Chart



# Empirical Proton Shell Gap



# Empirical Neutron Shell Gap

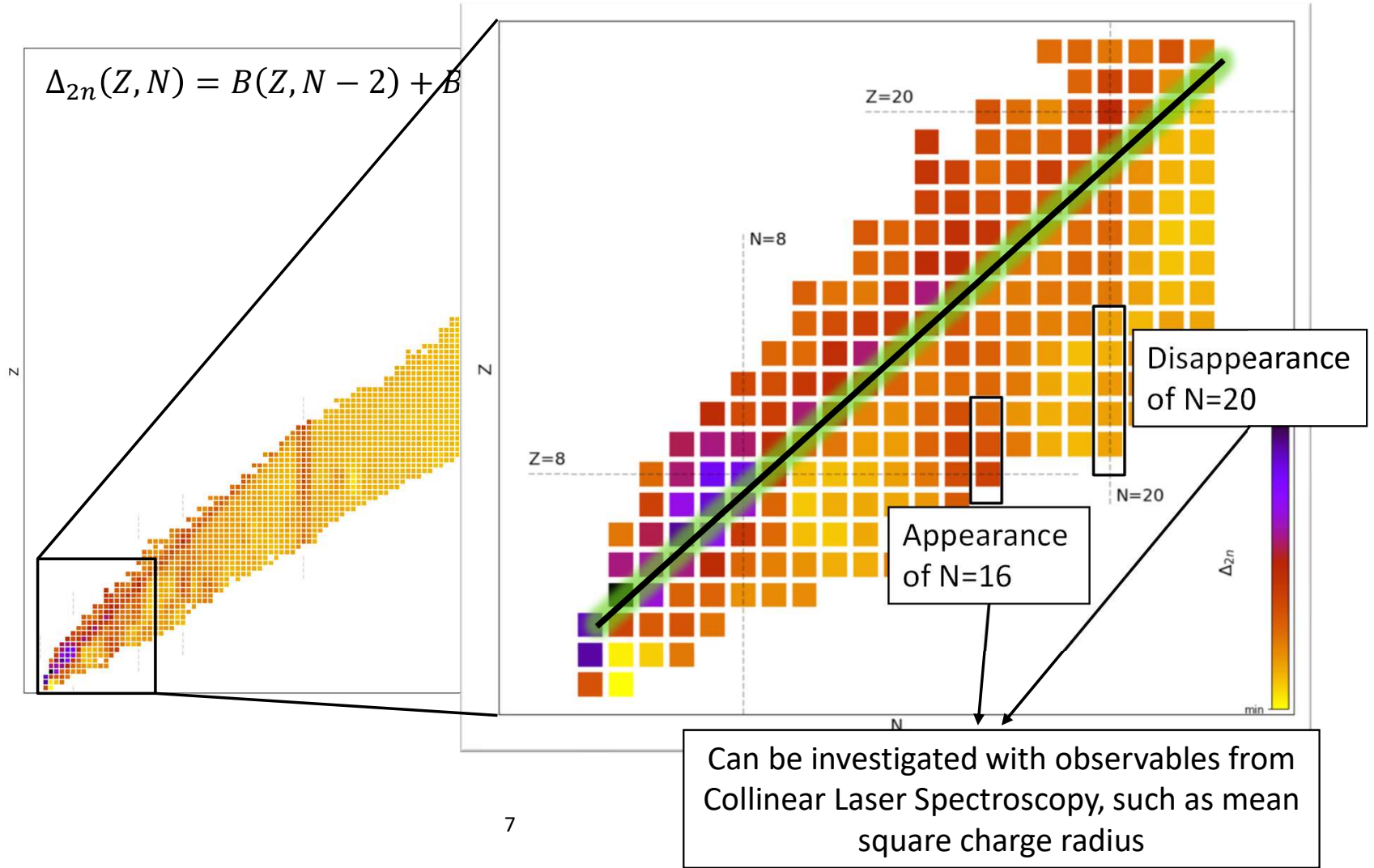


## Shell Model of Nuclei



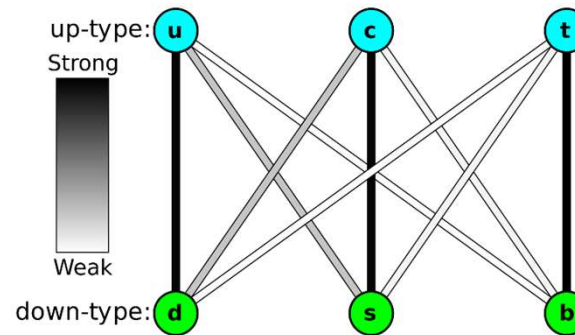
Maria Goeppert-Mayer  
 J. Hans D. Jensen  
 Nobel prize 1963

# Empirical Neutron Shell Gap



# Standard Model of Particle Physics

- Standard Model of particle physics
  - very successful theory in physics
  - predicts sub-atomic particles further comprised of 3 generations of quarks



- Cabibbo-Kobayashi-Maskawa (CKM) matrix describes mixing of quarks via weak interaction

$$V_{CKM} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$



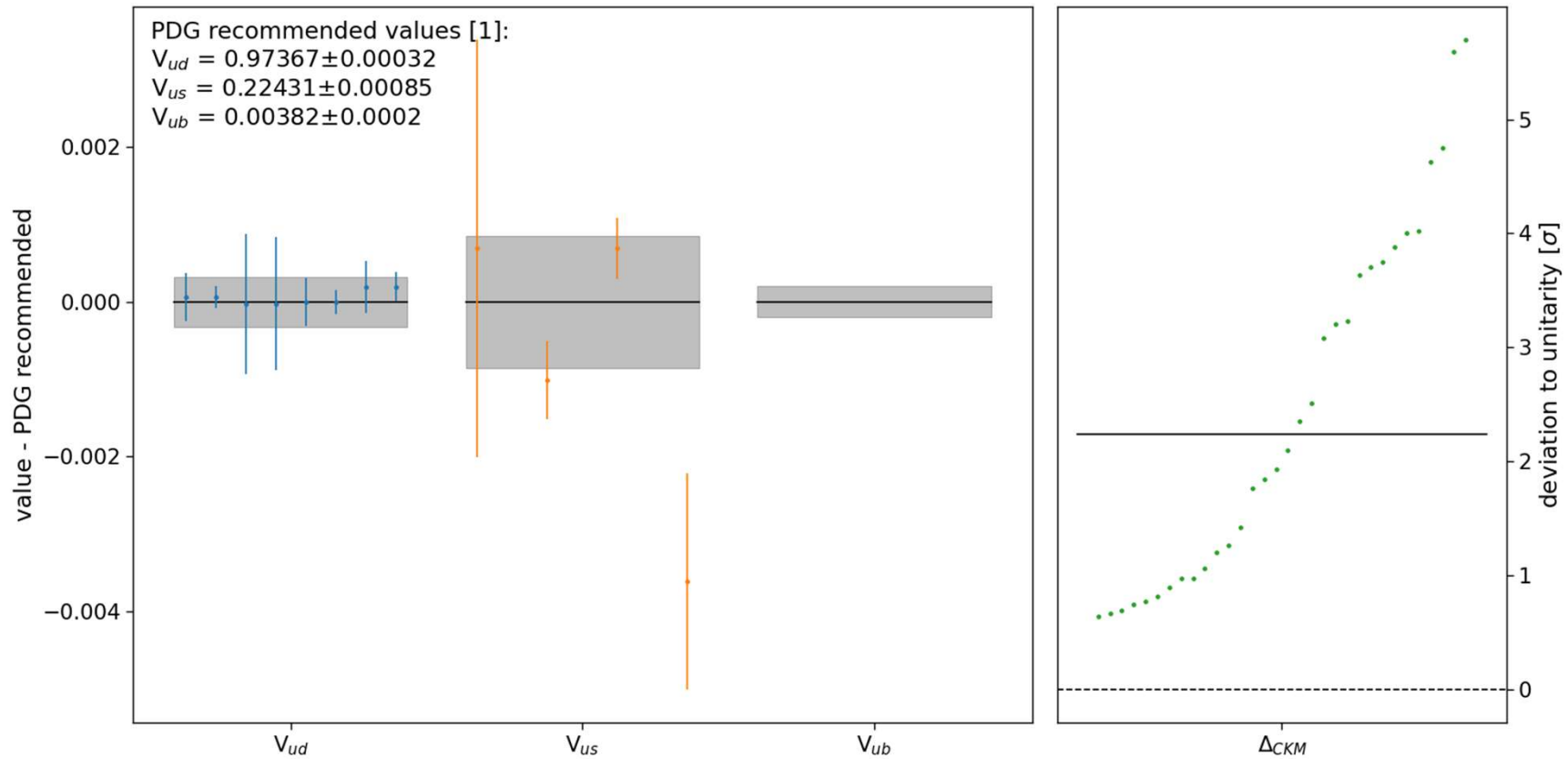
# CKM Unitarity

$$V_{CKM} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$

- Absolute square (i.e.  $|V_{ij}|^2$ ) of each CKM-entry is probability of weak decay of j-type quark into i-type quark
- Standard Model of particle physics predicts unitarity of CKM matrix
- Deviation from unitarity would imply incomplete picture of Standard model
  
- Unitarity:  $V_{CKM} \cdot V_{CKM}^T = I_3$
- In particular:  $|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 = 1$
- Deviation from unitarity:  $|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 = 1 - \Delta_{CKM}$

# Tension to Unitarity

- Currently recommended values by PDG:



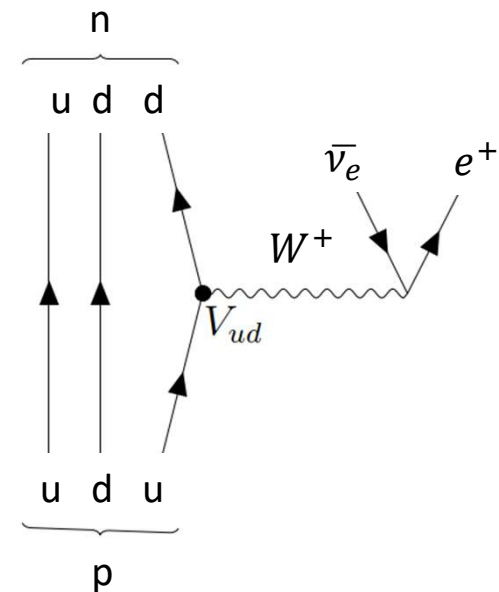
[1] S. Navas et al. (Particle Data Group), Phys. Rev. D 110, 030001 (2024)

[2] J. C. Hardy, I. S. Towner, Physical Review C 2020, 102.



# CKM Unitarity (2)

- Determination of couplings for:
- $V_{us}$ 
  - Kaon decays
  - Hyperon decays
  - Tau decays
- $V_{ud}$ 
  - Neutron decay
  - Pion decay
  - Mirror decays (e.g.  $^{21}\text{Na} \rightarrow ^{21}\text{Ne}$ )
  - **Superallowed  $0^+ \rightarrow 0^+$   $\beta$  decays**



# Determination of $V_{ud}$

- $V_{ud}$  can be determined via  $\mathcal{F}t$  value of superallowed  $0^+ \rightarrow 0^+$   $\beta$  decays

$$|V_{ud}|^2 = \frac{K}{2G_F^2(1 + \Delta_R^V)\overline{\mathcal{F}t}}$$

Partial half life

Energy difference

Small theoretical corrections  
(leading uncertainty!)

$$\mathcal{F}t = ft \cdot (1 + \delta'_R)(1 + \delta_{NS} - \delta_C)$$

- Nuclear charge radius  $r_c$  important experimental input into theoretical calculation of isospin-symmetry-breaking corrections

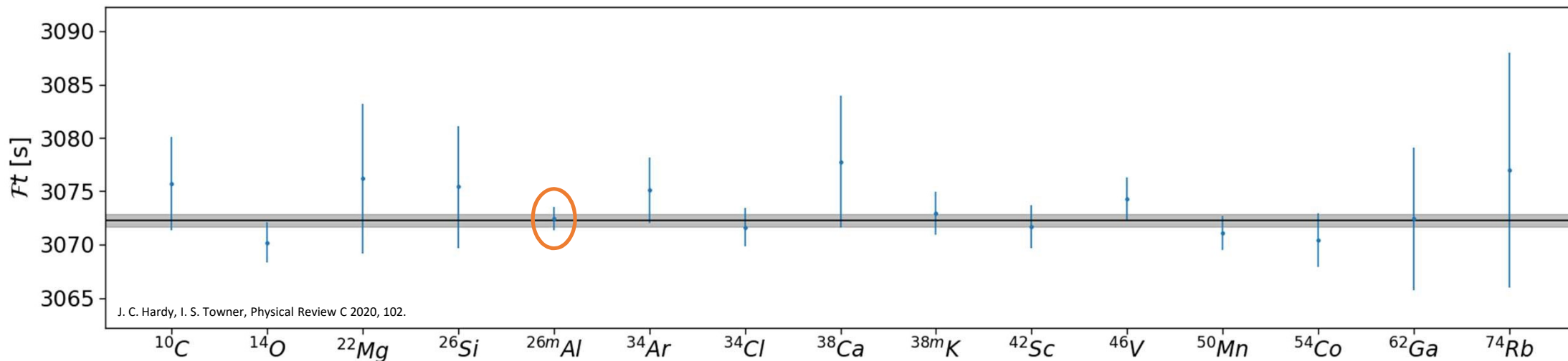
$$\delta_C := f(r_c, \dots)$$

# Importance of charge radius of $^{26m}\text{Al}$

- Weighted mean  $\overline{\mathcal{F}t}$  of 15 precision cases used to calculate  $V_{ud}$

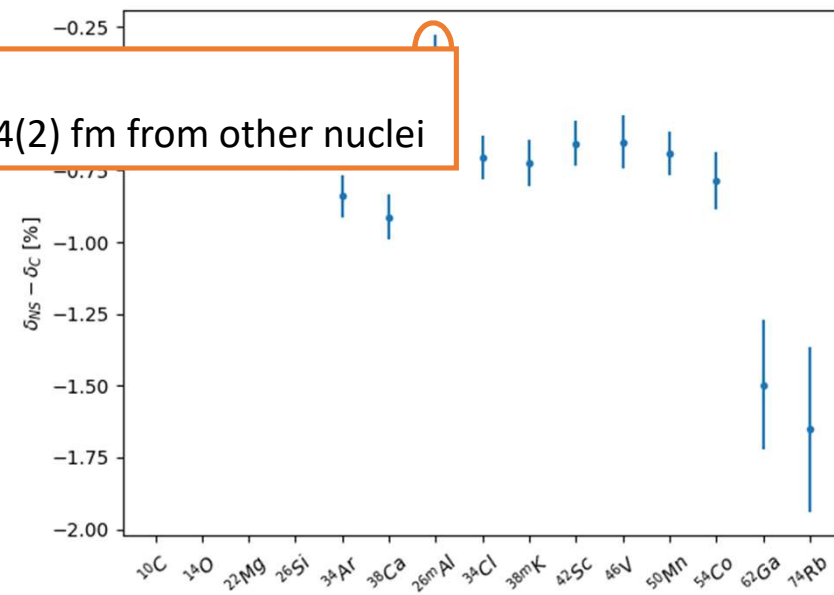
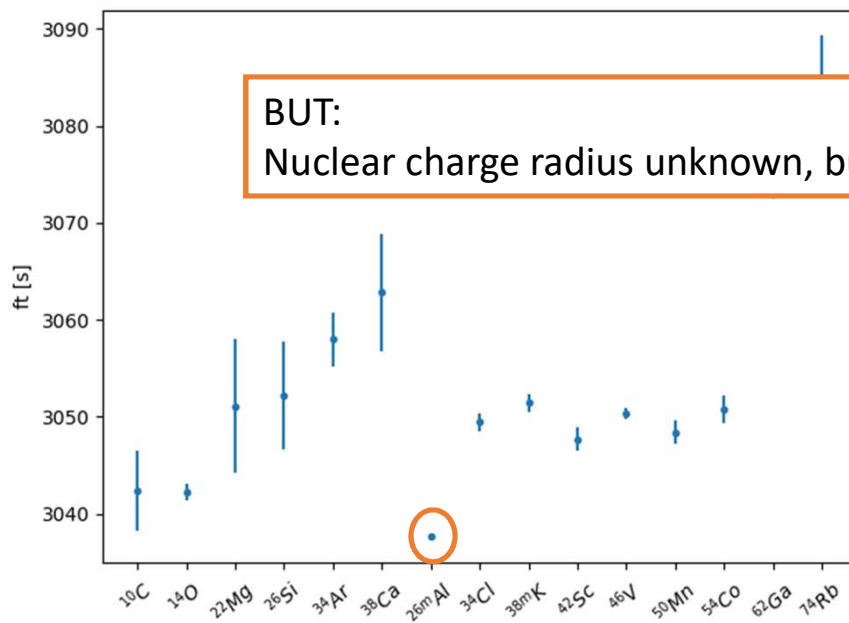
$$|V_{ud}|^2 = \frac{K}{2G_F^2(1 + \Delta_R^V)\overline{\mathcal{F}t}}$$

- $\mathcal{F}t$  value of  $^{26m}\text{Al}$ 
  - Most accurately known of 15 isotopes used to calculate  $\overline{\mathcal{F}t}$

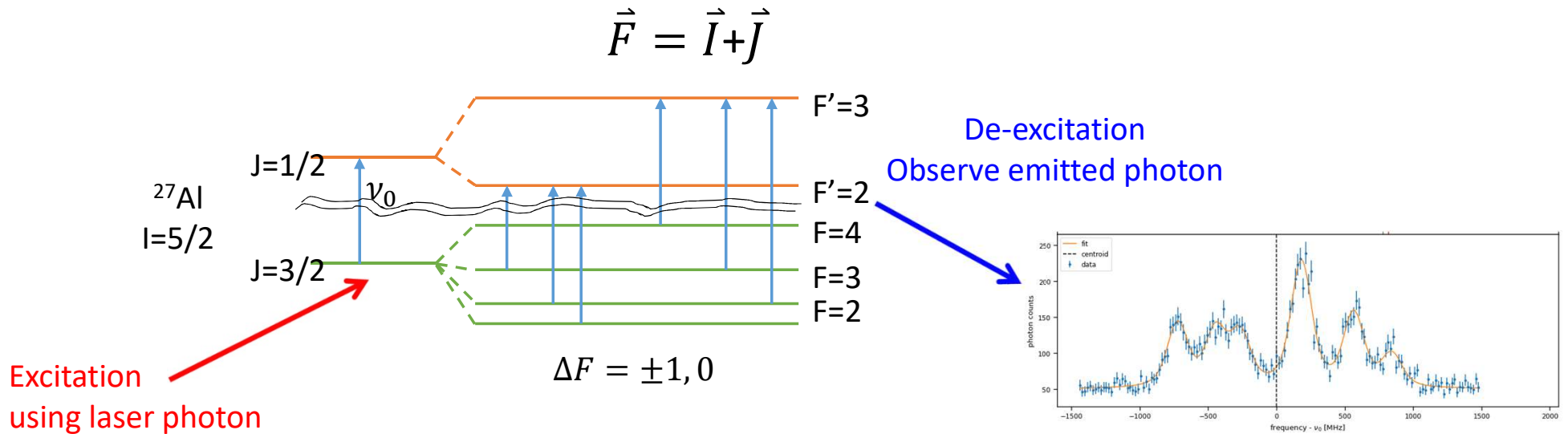


# Importance of charge radius of $^{26m}\text{Al}$

- Accuracy of  $\mathcal{F}t$  value of  $^{26m}\text{Al}$  coming from
  - Small uncertainty on  $ft$
  - Small uncertainty on nuclear structure and isospin-symmetry breaking corrections
  - Lowest numerical correction on combined  $\delta_{NS} - \delta_c$



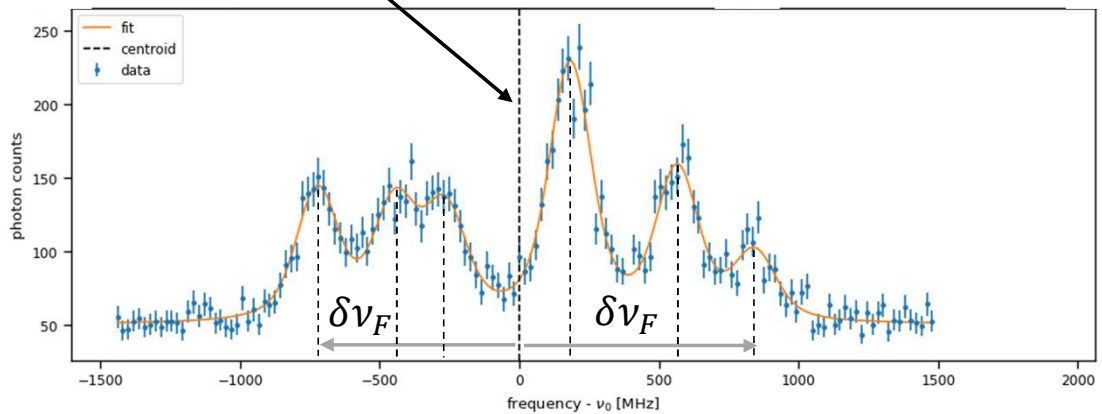
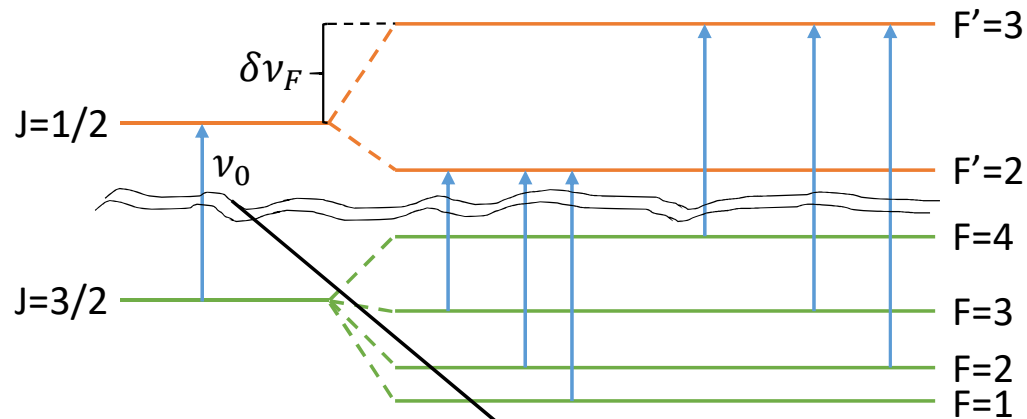
# Laser Spectroscopy



- Hyperfine transitions in atoms or ions yield information about
  - Nuclear spin
  - Magnetic dipole and electric quadrupole moments of nuclei
  - **Isotope shifts and nuclear charge radii**

# Hyperfine Spectrum

$^{27}\text{Al}$   
 $I=5/2$



$$\delta\nu_F = A_J \frac{C}{2} + B_J \frac{3C(C+1) - 4I(I+1)J(J+1)}{8I(2I-1)J(2J-1)}$$

$$C = F(F+1) - I(I+1) - J(J+1)$$

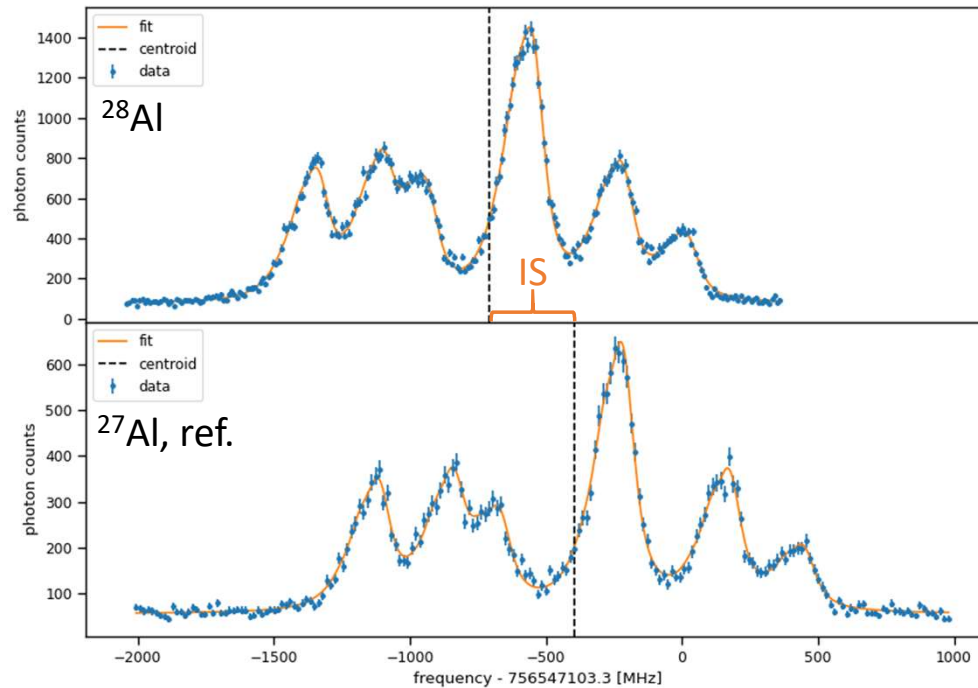
electric quadrupole moment  $Q = \frac{B_J}{eV_{JJ}}$

magnetic dipole moment  $\mu = \frac{A_J \cdot I \cdot J}{B_0}$

$$\delta\nu = \nu_0 + \delta\nu^{F'} - \delta\nu^F$$



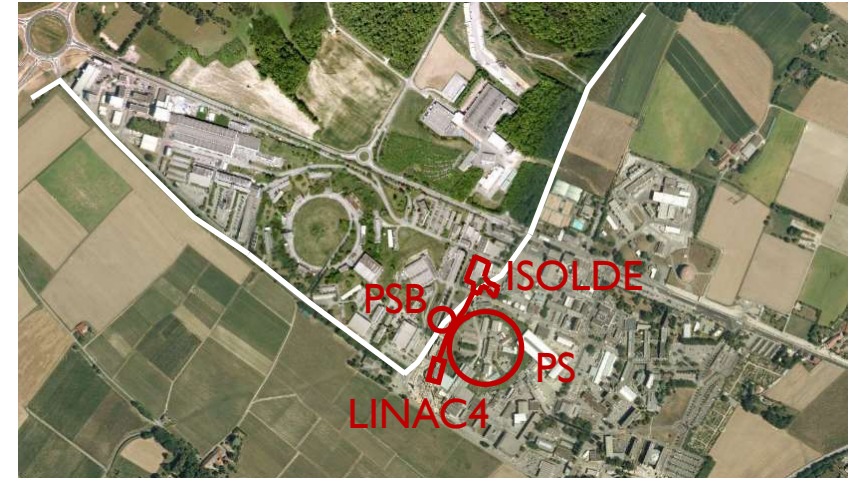
# Isotope Shift



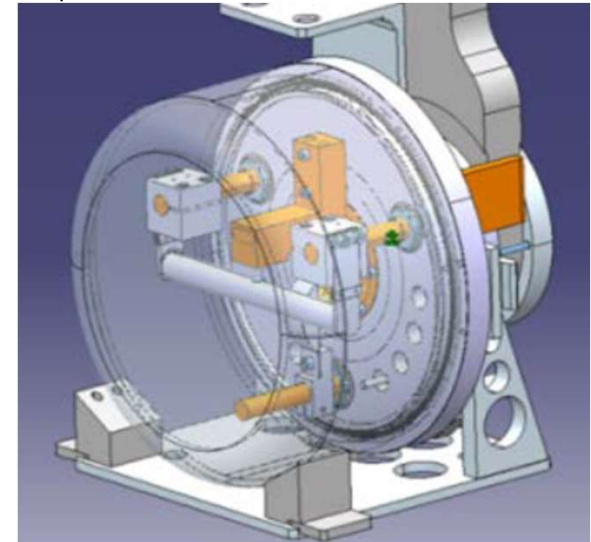
- Isotope shift  $IS = \text{difference of centroid frequencies for different isotopes}$
- Used to calculate difference in mean square charge radii between isotopes

# ISOLDE

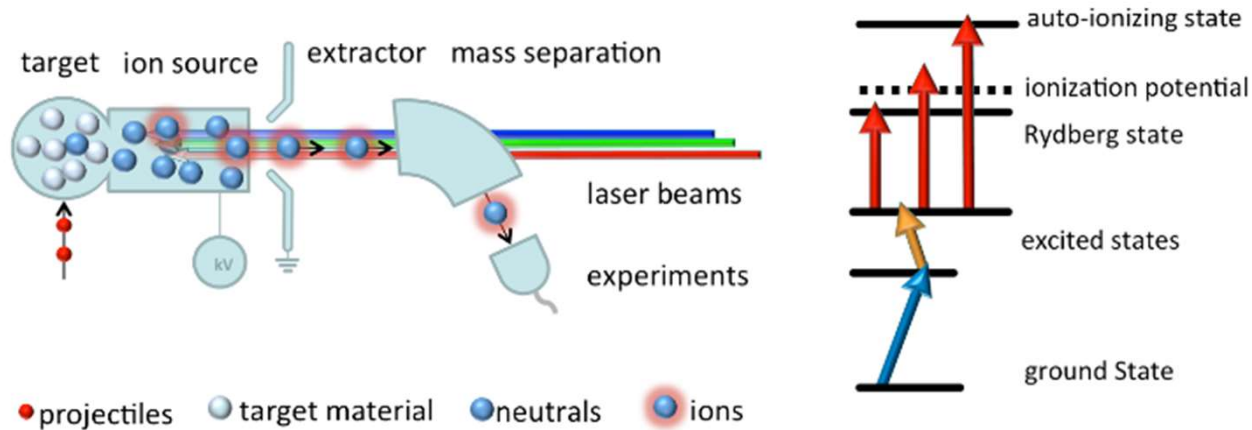
- Located at CERN
- Two target stations can be irradiated with up to 2  $\mu\text{A}$  of 1.4 GeV protons from proton synchrotron booster (PSB)
- Isotopes produced via nuclear reactions in target material
- Then ionised and transported to experimental setup



Source: <http://cds.cern.ch/record/1693046/files/arXiv:1404.0515.pdf>



# Ionisation

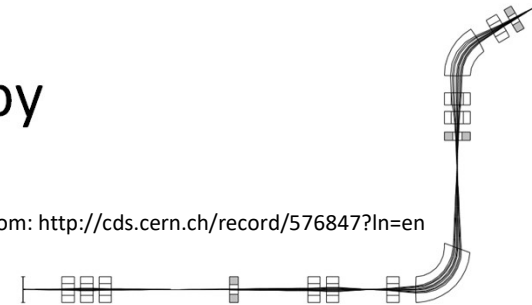


- Resonance ionisation laser ion source (RILIS)
- Electron excited through several resonant transition steps until ionization
- Very element specific
- Ionisation efficiency enhancement of factor  $\sim 10-100$  (varies for different schemes for different elements)

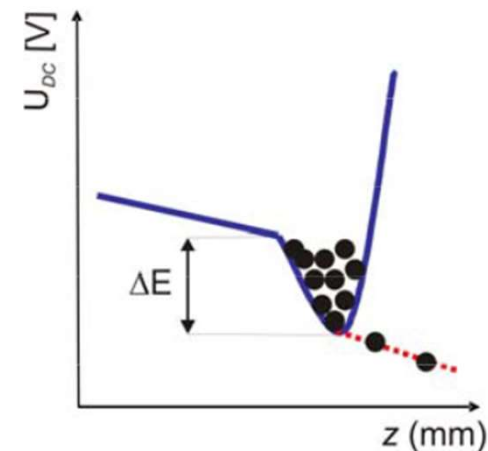
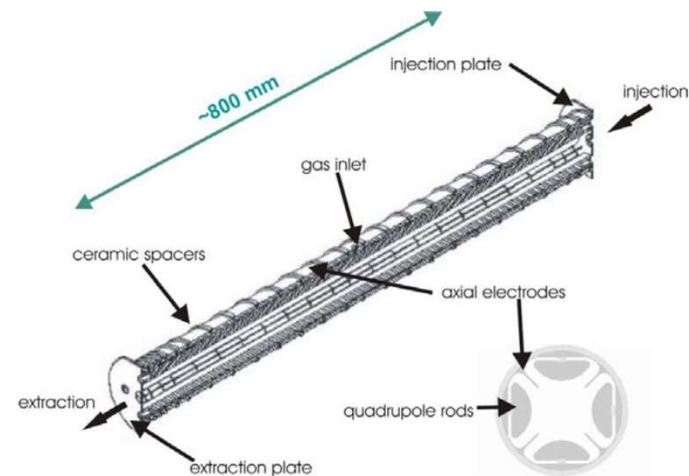
# Isotope Selection and Bunching

- Mass selection via High Resolution Separator (HRS) by two dipole magnets
- Offers mass resolving power of  $\sim 5000$
- Injected into helium buffer gas filled Paul trap (ISCOOL)
- Used as cooler-buncher to accumulate isotopes before transporting bunches to experiment

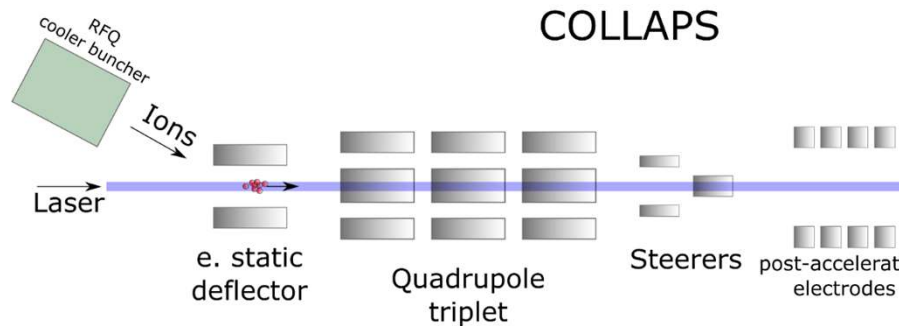
Image from: <http://cds.cern.ch/record/576847?ln=en>



Images from: <http://cds.cern.ch/record/1058103/files/p57.pdf>

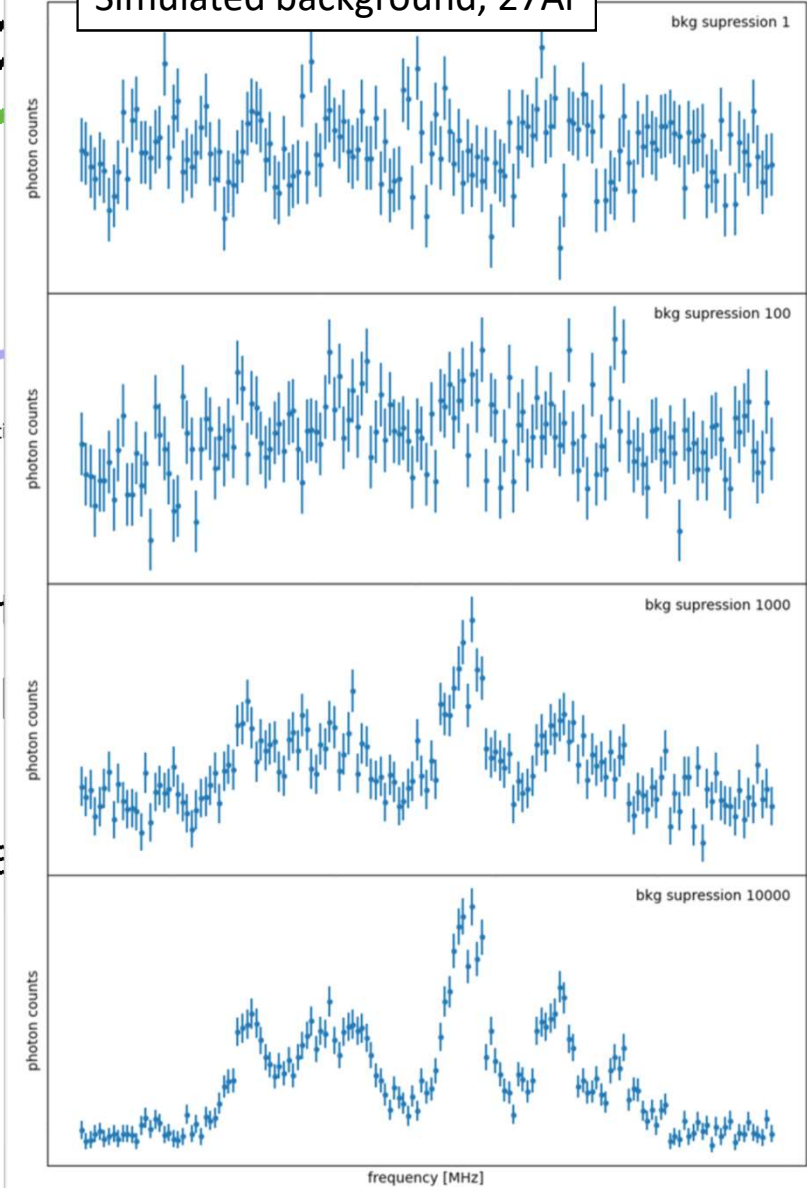


# Collinear Laser Spect

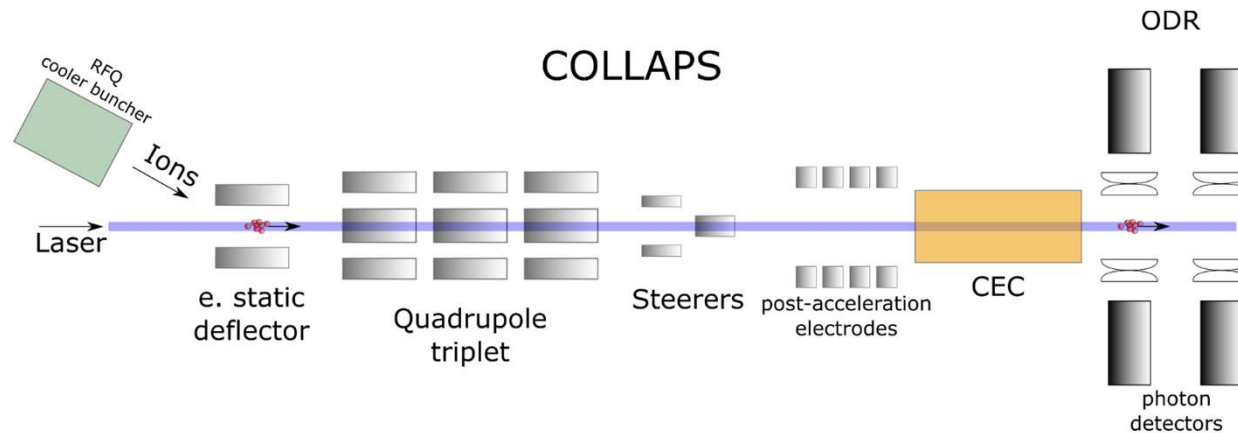


- Ions and laser collinearly overlapped via electrostatic deflection
- Reduced doppler spread ( $<100\text{MHz}$ ) due to “ $30\text{keV}$ ”
- Bunched beam allows for time gating to increase signal to background by factor of  $\sim 10\,000$

Simulated background,  $^{27}\text{Al}$

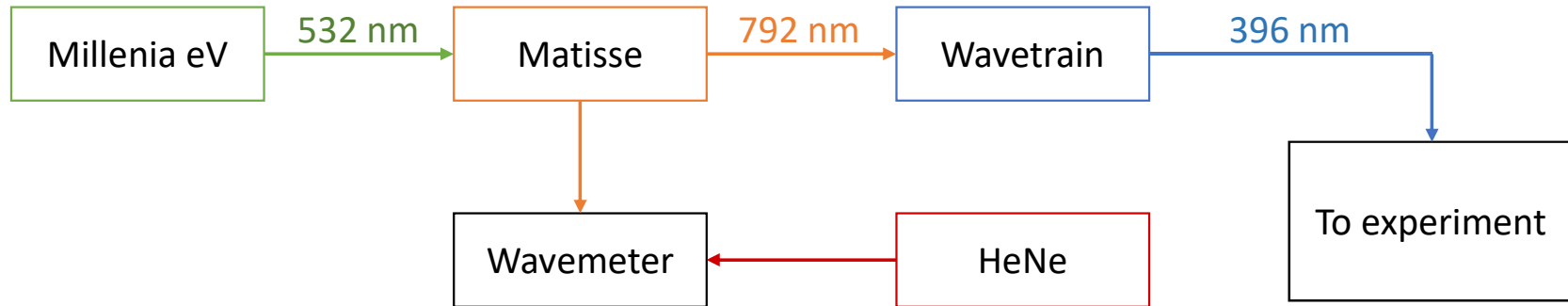


# Collinear Laser Spectroscopy

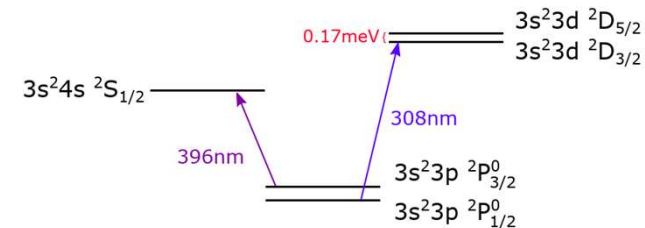


- Post-acceleration leads to frequency shift in ion rest frame
- Charge exchange with sodium to neutralize ions
- Measure fluorescence photons of resonant transitions

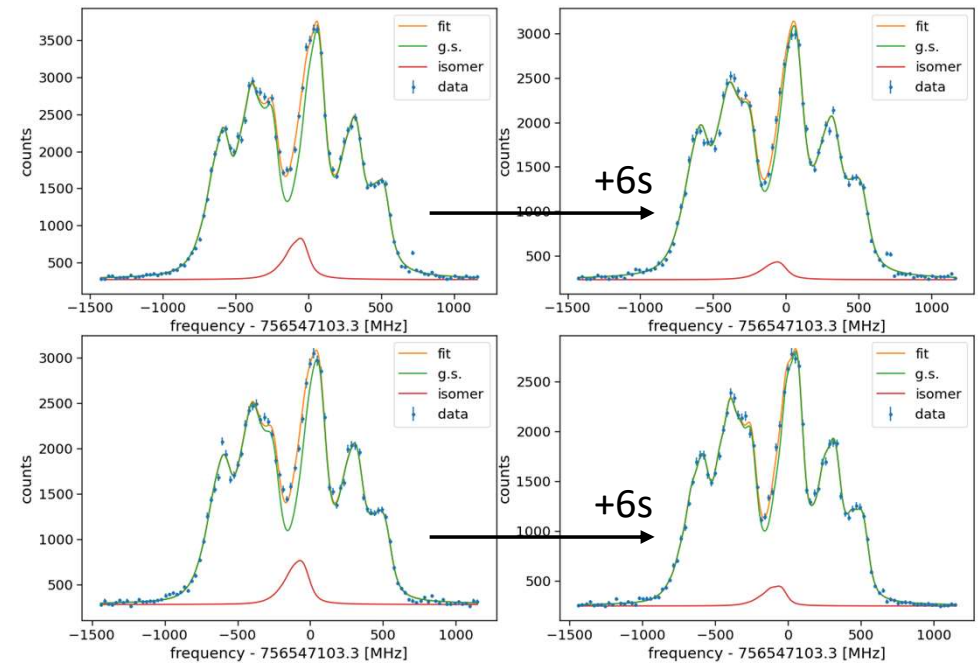
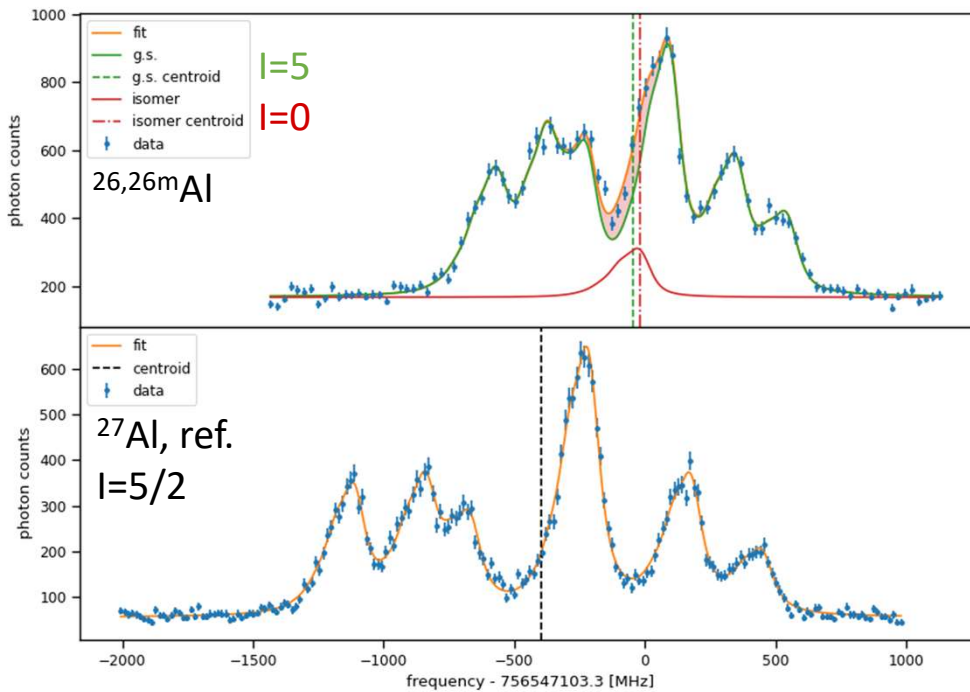
# Laser System



- Used transition:  $3s^23p\ ^2P_{3/2}^o \rightarrow 3s^24s\ ^2S_{1/2}$  provided by frequency doubled Matisse Ti:Sa ring cavity laser
- Frequency stabilised by WSU-10 wavemeter
- Regularly calibrated by HeNe laser



# Hyperfine Spectra

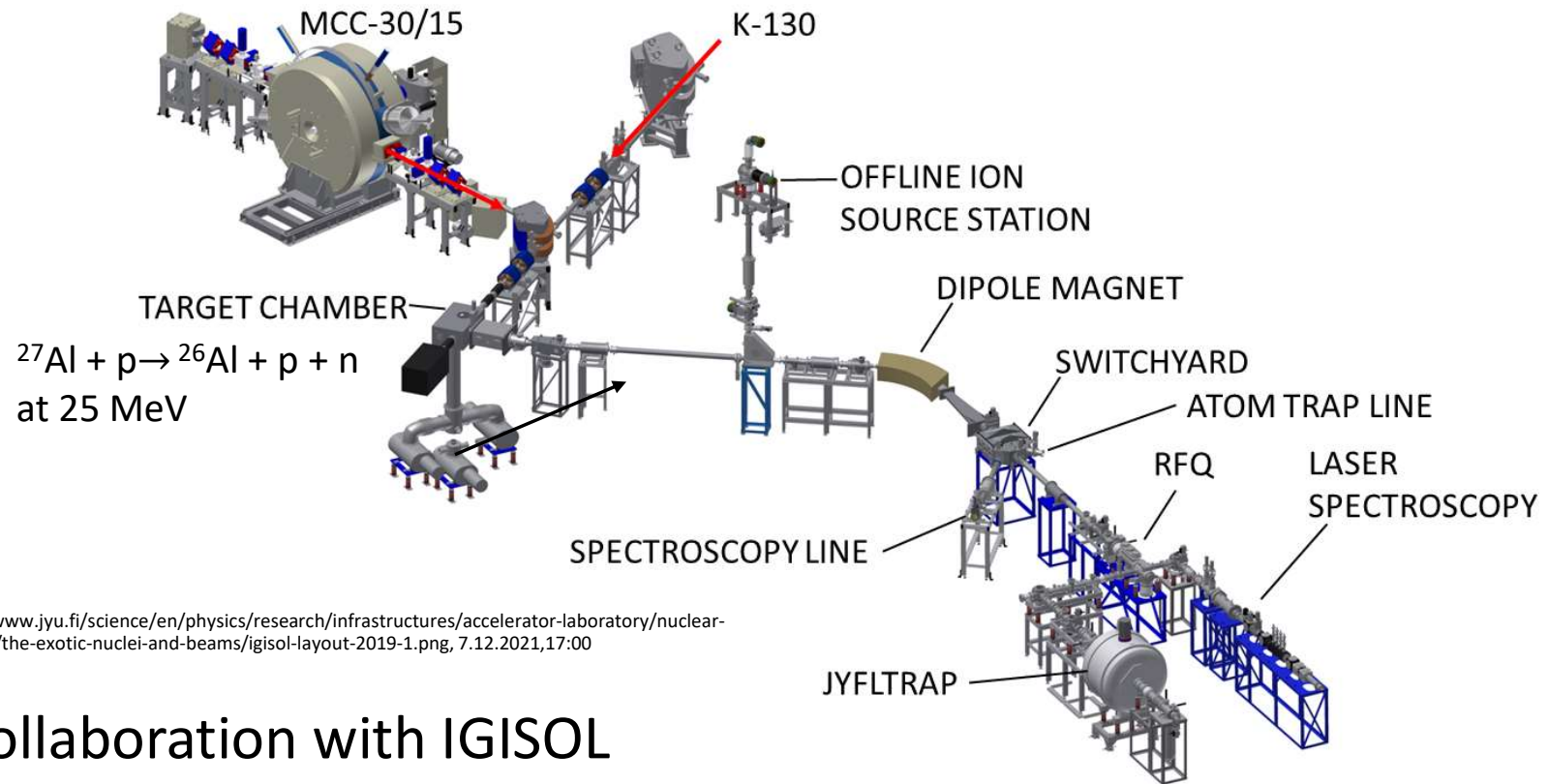


- Ion extraction 0 and 6s after proton trigger
- Decrease in isomer intensity in fit consistent with half-life

$$\triangleright N_2 = N_1 \cdot \left(\frac{1}{2}\right)^{\frac{6s}{t_{1/2}}}$$



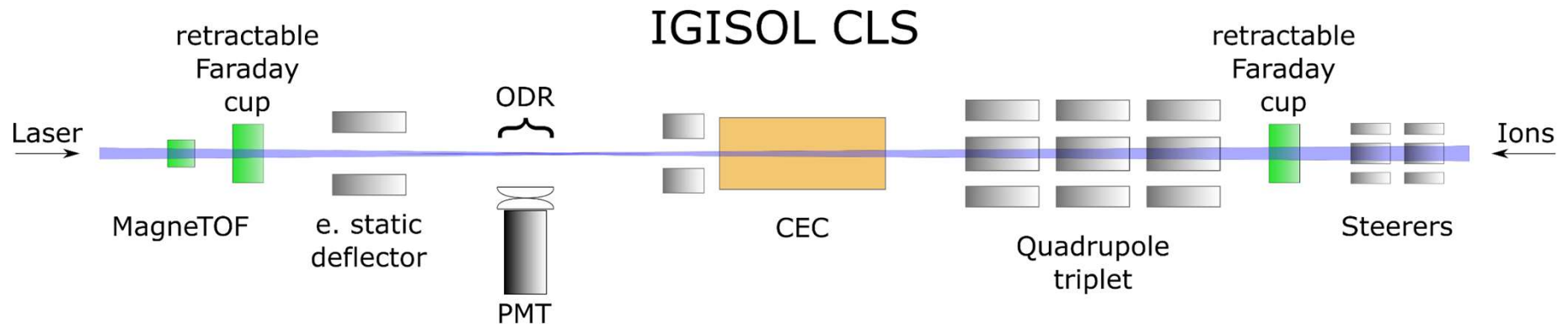
# IGISOL



Source: <https://www.jyu.fi/science/en/physics/research/infrastructures/accelerator-laboratory/nuclear-physics-facilities/the-exotic-nuclei-and-beams/igisol-layout-2019-1.png>, 7.12.2021,17:00

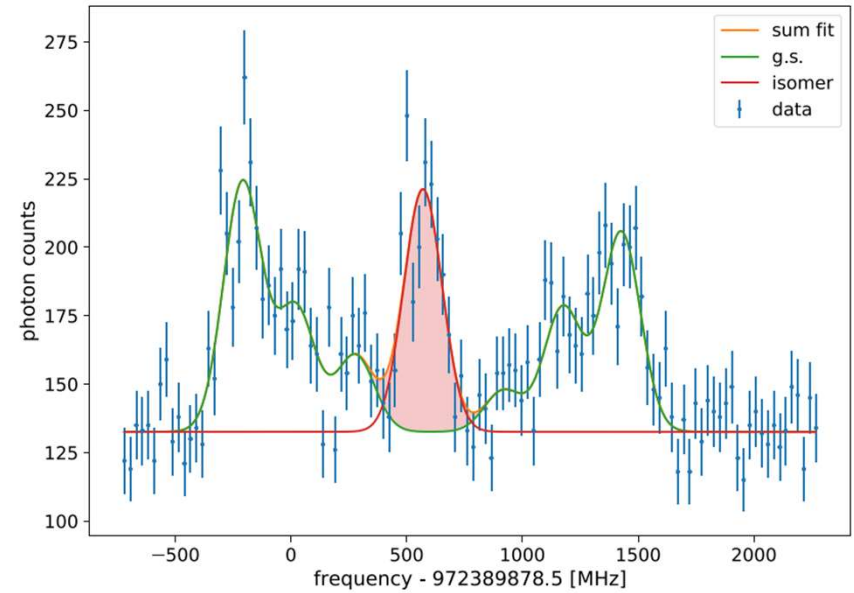
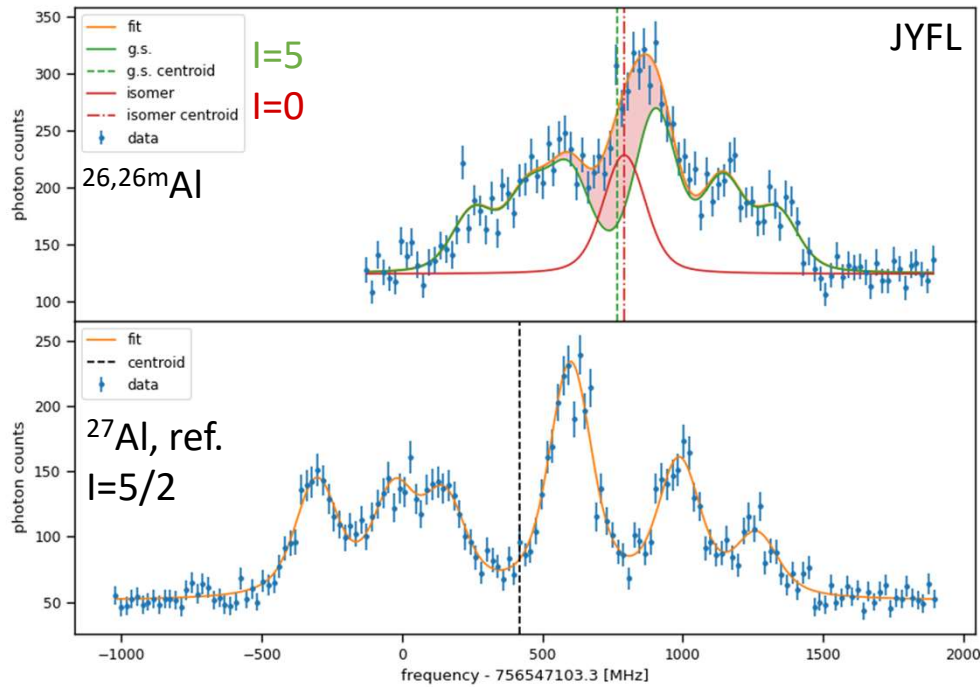
- Collaboration with IGISOL
- Second set of measurements performed at IGISOL, Jyväskylä
- Known to have more favorable isomer : ground state ratio for  $^{26,26\text{m}}\text{Al}$

# Collinear Laser Spectroscopy at IGISOL

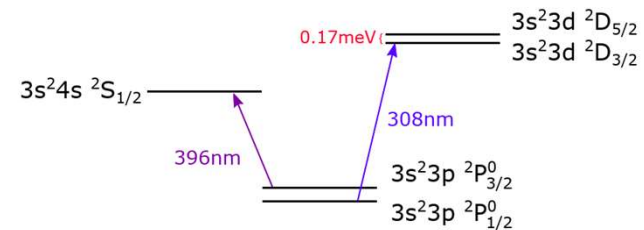


- Similar overall configuration as COLLAPS
- Laser and ions injected anti-collinearly
- CEC also filled with sodium
- Single photomultiplier compared to quad configuration at COLLAPS

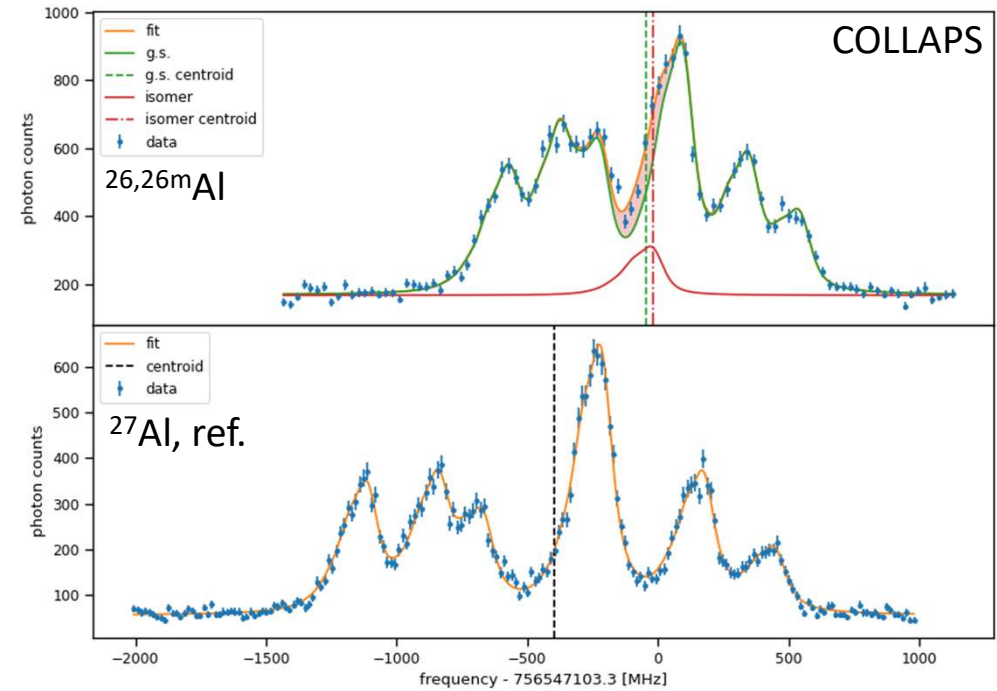
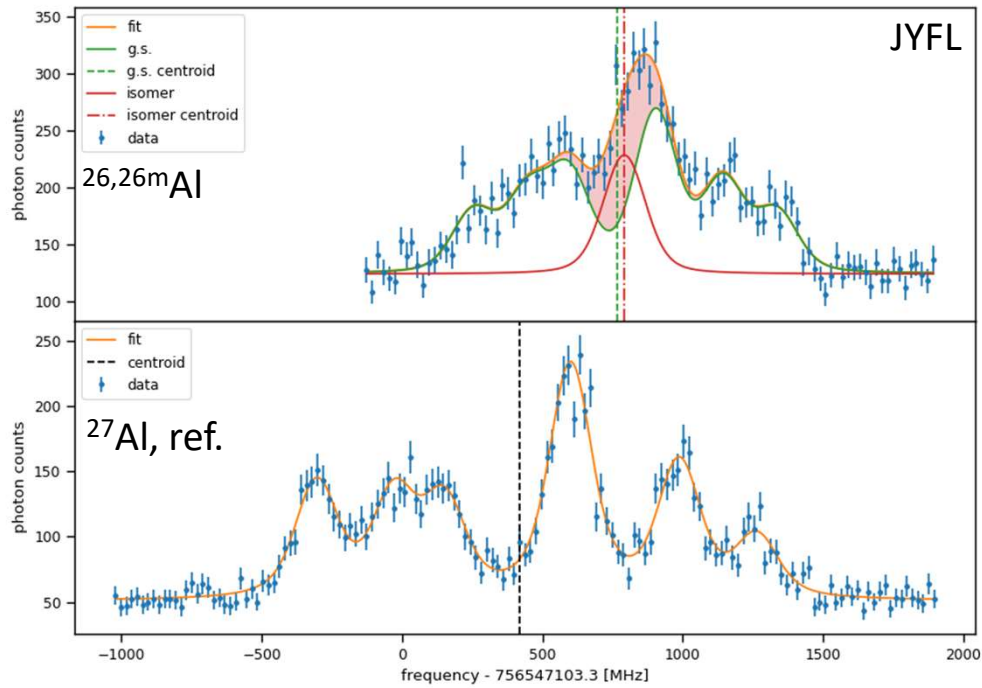
# Hyperfine Spectra



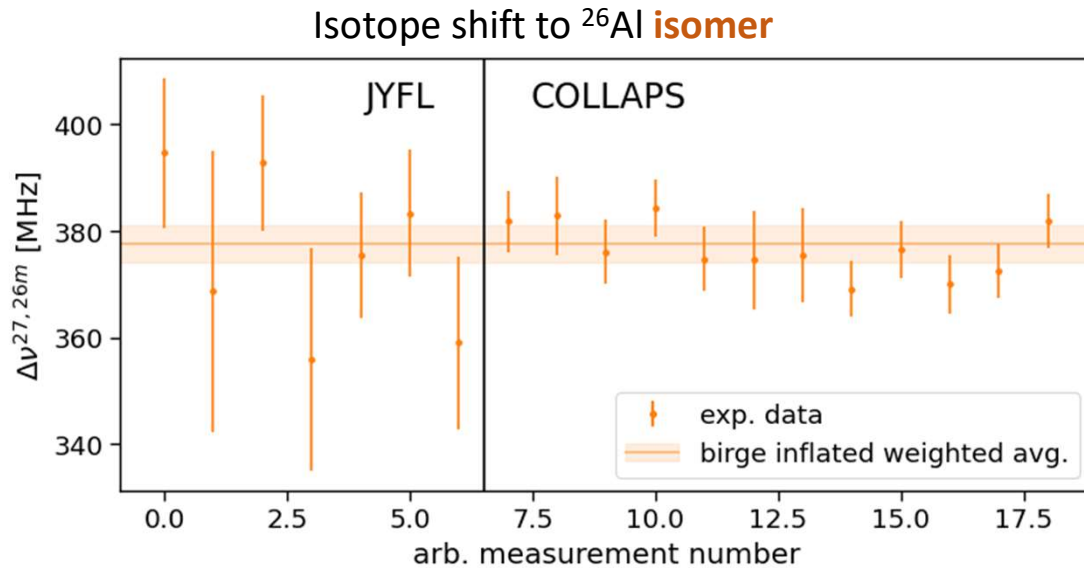
- Clear presence of isomer in  $\text{Al } | P_{1/2} \rightarrow D_{3/2}$  transition



# Hyperfine Spectra



# Isotope Shift



Isotope Shift [MHz]	
IGISOL	379.7{5.5}[2.2]
COLLAPS	376.5{1.7}[3.7]
weighted avg.	377.5(3.4)

- Statistical and systematic uncertainties combined in quadrature for each experiment
- Combination of both datasets as weighted average

# Mean Square Charge Radius

- Isotope shifts  $\delta\nu^{27,26}$ ,  $\delta\nu^{27,26m}$  used to calculate difference in mean square nuclear charge radii  $\delta\langle r^2 \rangle^{27,A}$  between  $^{26,26m}\text{Al}$  and  $^{27}\text{Al}$  reference

$$\delta\langle r^2 \rangle^{27,A} = \frac{\delta\nu^{27,A}}{F} - \frac{M}{F} \frac{m_A - m_{27}}{m_{27} \cdot (m_A + m_e)}$$

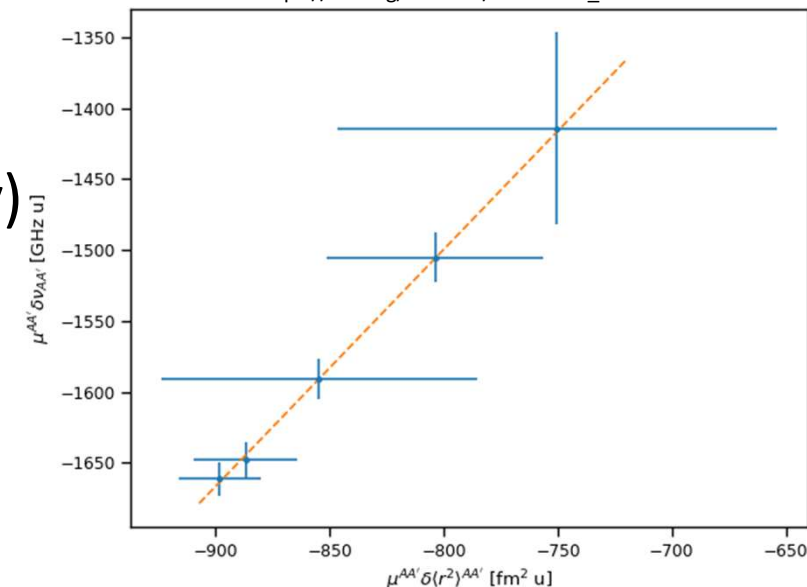
- Depends on
  - Respective nuclear masses  $m_A$ , electron mass  $m_e$
  - Atomic mass shift factor M
  - Field shift factor F

# King plot

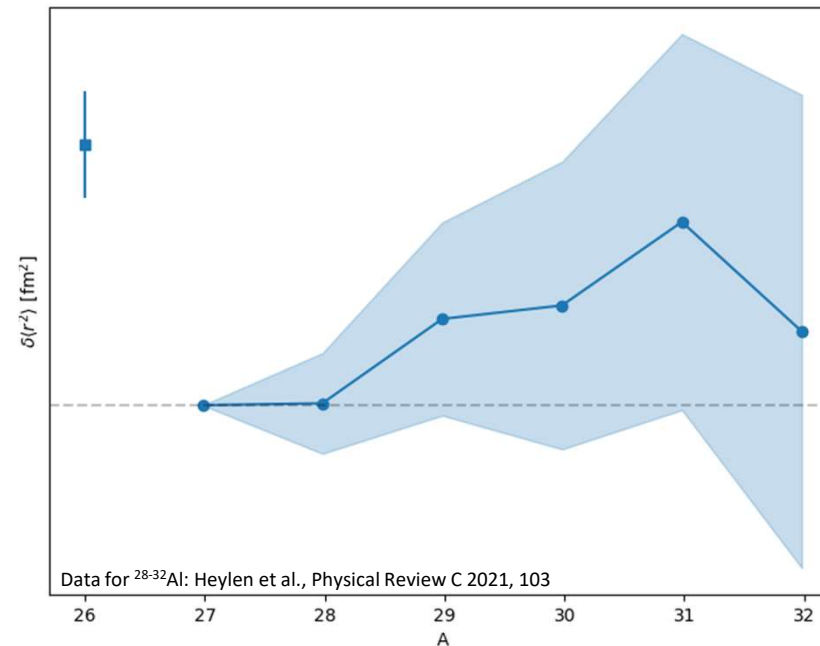
- If enough ( $\geq 3$ ) stable isotopes with absolute charge radii are known
- Transformation of previous equation leads to linear relation  $\mu_{27,A} \cdot \delta v^{27,A} = F \cdot \mu_{27,A} \cdot \delta \langle r^2 \rangle^2 + M$
- Aluminium: only 1 stable isotope
- Determination of F and M through atomic calculations necessary (higher uncertainty)

$$\mu_{27,A} := \frac{m_{27} \cdot (m_A + m_e)}{m_A - m_{27}}$$

Example: isotopes of tin  
 Source IS: PRL 122, 192502 (2019)  
 Source radii: [https://doi.org/10.1007/10856314\\_1](https://doi.org/10.1007/10856314_1)



# RMS Charge Radii of aluminium isotopes



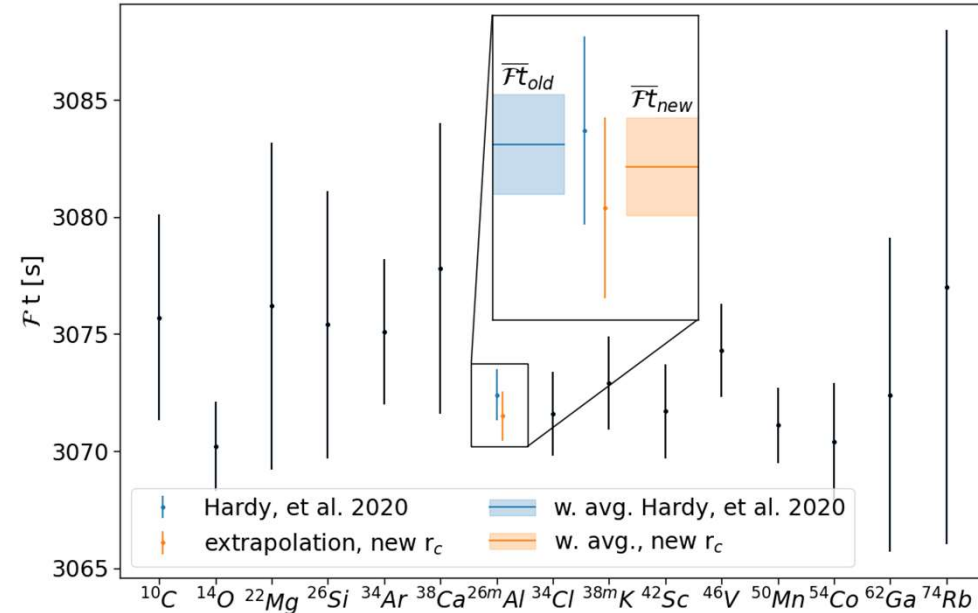
- Absolute charge radius of  $^{27}\text{Al}$  from Barrett equivalent radius obtained by muonic spectroscopy and charge density from electron scattering measurements



# Nuclear Charge Radius and $\mathcal{F}t$

- Nuclear charge radius of  $^{26}\text{mAl}$ : 3.130(15) fm
- 4.5 statistical standard deviations from extrapolated value
- First extrapolation by same number of standard deviations for radial overlap correction of ISB correction

	Old values from [1]	New Values
$^{26}\text{mAl}$ nuclear charge radius	3.04(2) fm	3.130(15) fm
$\mathcal{F}t$ of $^{26}\text{mAl}$	3072.4(1.1) s	3071.4(1.0) s
$\overline{\mathcal{F}t}$	3072.24(1.85) s	3071.96(1.85) s



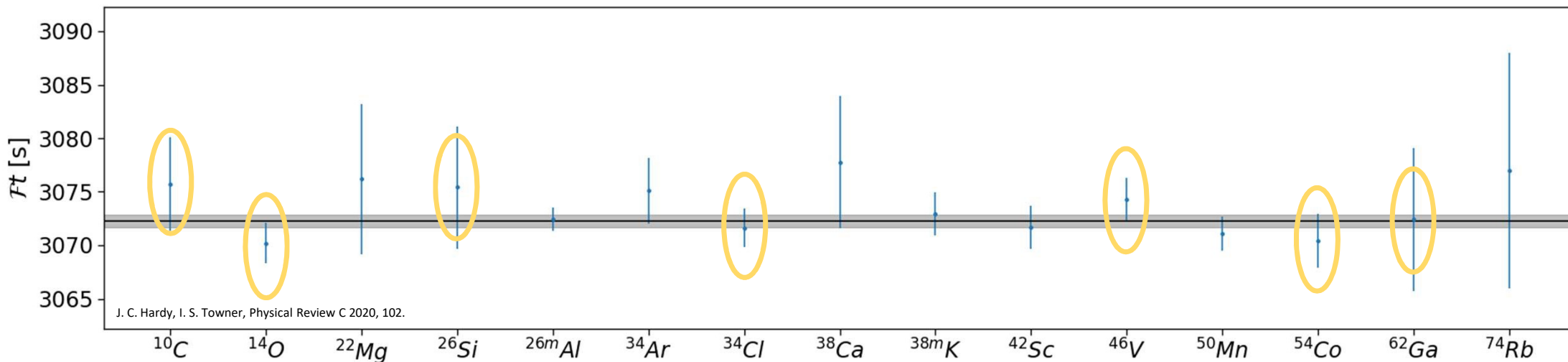
[1] J. C. Hardy, I. S. Towner, Physical Review C 2020, 102.

# Implications for CKM unitarity

- Shifts the result of unitarity test closer towards unitarity by  $\sim 1/10$  standard deviations

$$|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 = 0.99848(70) \rightarrow 0.99856(70)$$

- Motivates further studies of nuclear charge radii in other superallowed  $\beta$  emitters with so-far unknown charge radii:

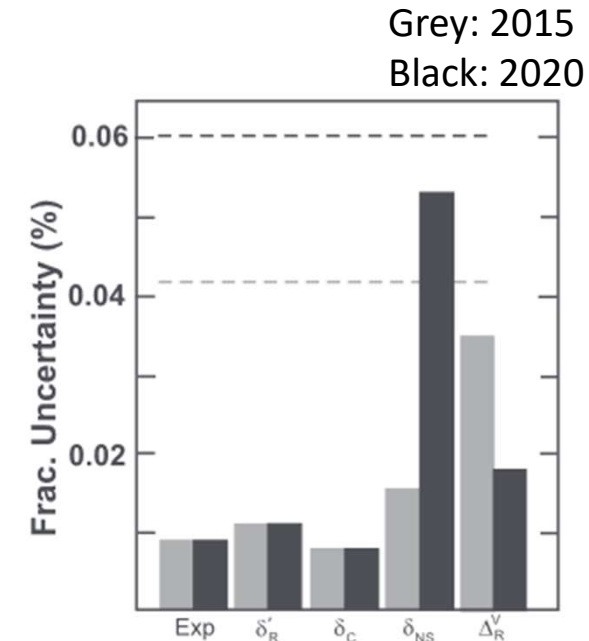


# Outlook

- Current status: charge radii of 7/15 superallowed beta emitters still unknown
- Ongoing efforts to determine  $^{54}\text{Co}$  at IGISOL
- Further effect of charge radius of  $^{26\text{m}}\text{Al}$  on Fermi function leading to necessary correction of  $ft$ -value
- → Might result in another shift of average  $\mathcal{F}t$  depending on magnitude of correction

# Outlook

- Uncertainty of  $|V_{ud}|^2$  currently dominated by systematic theoretical uncertainties on  $\delta_{NS}$
- If  $\delta_{NS}$  were reduced to being non-dominant contribution, result of unitarity test would shift to  $\approx 3\sigma$
- New calculations for  $\delta_{NS}$  correction (with ab-initio methods) are being explored by TRIUMF's theory department
- Currently limited to lightest superallowed  $\beta$  emitters



Source: J. C. Hardy, I. S. Towner, Physical Review C 2020, 102.

# Summary and Conclusion

- The charge radius of  $^{26\text{m}}\text{Al}$  has been determined by Collinear Laser spectroscopy
- 4.5 standard deviations difference to extrapolated value used in isospin-symmetry-breaking corrections for  $V_{ud}$  of CKM matrix
- Extrapolation points towards slight shift towards CKM unitarity
- For more information:  
PRL 131, 222502 (2023) (DOI:10.1103/PhysRevLett.131.222502)

# Thank you for your attention!

P. PLATTNER<sup>1</sup>, E. WOOD<sup>2</sup>, L. AL AYOUBI<sup>3</sup>, O. BELIUSKINA<sup>3</sup>, M. L. BISSELL<sup>4,5</sup>, K. BLAUM<sup>1</sup>, P. CAMPBELL<sup>4</sup>, B. CHEAL<sup>2</sup>, R. DE GROOTE<sup>6</sup>, C. DEVLIN<sup>2</sup>, T. ERONEN<sup>3</sup>, L. FILIPPIN<sup>7</sup>, R. F. GARCÍA RUZÍZ<sup>8</sup>, Z. GE<sup>3</sup>, S. GELDHOF<sup>6</sup>, W. GINS<sup>3</sup>, M. GODEFROID<sup>7</sup>, H. HEYLEN<sup>5</sup>, M. HUKKANEN<sup>3</sup>, J. D. HOLT<sup>9,10</sup>, P. IMGAM<sup>11</sup>, A. JARIES<sup>3</sup>, A. JOKINEN<sup>3</sup>, A. KANELLAKOPOULOS<sup>6</sup>, A. KANKAINEN<sup>3</sup>, S. KAUFMANN<sup>11</sup>, K. KÖNIG<sup>11</sup>, Á. KOSZORÚS<sup>5</sup>, S. KUJANPÄÄ<sup>3</sup>, S. LECHNER<sup>5</sup>, S. MALBRUNOT-ETTENAUER<sup>5</sup>, R. MATHIESON<sup>2</sup>, T. MIYAGI<sup>11</sup>, I. MOORE<sup>3</sup>, P. MÜLLER<sup>11</sup>, D. NESTERENKO<sup>3</sup>, R. NEUGART<sup>1,12</sup>, G. NEYENS<sup>6</sup>, W. NÖRTERSCHÄUSER<sup>11</sup>, A. ORTIZ-CORTES<sup>3</sup>, H. PENTTILÄ<sup>3</sup>, I. POHJALAINEN<sup>3</sup>, A. RAGGIO<sup>3</sup>, M. REPONEN<sup>3</sup>, S. RINTA-ANTILA<sup>3</sup>, L. V. RODRÍGUEZ<sup>5,1</sup>, J. ROMERO<sup>3</sup>, R. SÁNCHEZ<sup>13</sup>, F. SOMMER<sup>11</sup>, M. STRYJCZYK<sup>3</sup>, V. VIRTANEN<sup>3</sup>, L. XIE<sup>4</sup>, Z. Y. XU<sup>6</sup>, X. F. YANG<sup>6,14</sup>, AND D. T. YORDANOV<sup>15</sup>

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